

Integrable Systems: Geometrical and Analytical Approaches

Report of Contributions

Contribution ID: 3

Type: **Lecture**

Asymptotic analysis of integrable dispersive PDEs: random multisoliton solutions

Thursday, June 6, 2024 11:50 AM (50 minutes)

I will present a series of examples of soliton gasses, in which the interplay of Riemann-Hilbert analysis and randomness provides a detailed description of interesting phenomena. Time will be reserved to discuss future research challenges. Our research group includes Manuela Girotti (Emory), Aikaterini Gkogkou (Tulane), Tamara Grava (SISSA), Robert Jenkins (University of Central Florida), Guido Mazzuca (Tulane), Alexander Minakov (Prague), and Maxim Yattselev (IUPUI), and I will be sampling from work with various subsets of the team.

Primary author: MCLAUGHLIN, Kenneth (Tulane University)

Presenter: MCLAUGHLIN, Kenneth (Tulane University)

Contribution ID: 4

Type: **Lecture**

Bargmann gas solution to the mKdV equation

Thursday, June 6, 2024 11:00 AM (50 minutes)

We construct a new class of (gas) solutions of the mKdV equation as a limit of $2N$ solitons, eventually in the presence of an additional dispersive coefficient. We also analyze the long-time behaviour of the profile: the solution is asymptotically an elliptic solution at both $x \rightarrow \pm\infty$, with same parameters, but different shift x_0^\pm .

This is a joint work with Ken McLaughlin (Tulane U.) and Robert Jenkins (UCF).

Primary author: GIROTTI, Manuela (Emory University)

Presenter: GIROTTI, Manuela (Emory University)

Contribution ID: 6

Type: **Lecture**

Exactly solvable interacting particle systems

Tuesday, June 4, 2024 11:50 AM (50 minutes)

In statistical physics systems of interacting particles can be used as toy models to study non equilibrium phenomena. A way to do that is to place the system in contact with an external environment that generates a current through it, place the system out of equilibrium and so reversibility is lost. In these boundary driven models the first natural question one would like to answer regards the stationary measure: stationary states are considered the simplest beyond equilibrium but are, in general, not known explicitly. I will present two models recently introduced where the stationary measure can be obtained.

Joint work with: Gioia Carinci, Rouven Frassek, Davide Gabrielli, Cristian Giardinà, Frank Redig, Dimitrios Tsagkarogiannis.

Primary author: FRANCESCHINI, Chiara (UniMoRe)

Presenter: FRANCESCHINI, Chiara (UniMoRe)

Contribution ID: 7

Type: **Lecture**

On some tautological relations between decorated trees and the DR/DZ conjecture

Friday, June 7, 2024 11:00 AM (50 minutes)

We study some relations between trees decorated by the double ramification cycles times λ_g and trees decorated by the Omega class, via virtual localisation. We then employ virtual localisation to deduce some polynomiality properties of the Omega class. If time permits, some connections with the DR/DZ conjecture will be discussed.

Primary author: Dr LEWANSKI, Danilo

Presenter: Dr LEWANSKI, Danilo

Contribution ID: 8

Type: **Lecture**

Bi-flat F-manifolds, Frolicher Nijenhuis Bicomplexes and Integrable Systems

Friday, June 7, 2024 11:50 AM (50 minutes)

We introduce some geometric structures related to the notion of bi-flat F-manifolds and we show their applications to the theory of Integrable Systems.

Based on joint works with Alessandro Arsie, Franco Magri and Sara Perletti.

Primary author: LORENZONI, Paolo (Università di Milano-Bicocca)

Presenter: LORENZONI, Paolo (Università di Milano-Bicocca)

Contribution ID: 9

Type: **Lecture**

Gradient blowups in multidimensional Burgers-Hopf equation

Tuesday, June 4, 2024 2:30 PM (50 minutes)

The dust equation, also known as homogeneous or pressureless Euler equation (Zel'dovich, 1970), is a toy-model for the fluid dynamic Euler equation in which pressure is neglected. This PDE is the multidimensional analogue of the Burgers-Hopf equation and is a good training ground for the analysis of the catastrophe structures in more than one spatial dimension. In the talk, the gradient blowups for this model are characterized with particular attention to the behavior of the vorticity and the effects of external fields.

Primary author: ORTENZI, Giovanni (Università di Milano Bicocca)

Presenter: ORTENZI, Giovanni (Università di Milano Bicocca)

Contribution ID: 10

Type: **Lecture**

Maxwell–Bloch equations without spectral broadening: the long-time asymptotics of an input pulse in a long two-level laser amplifier

Tuesday, June 4, 2024 3:20 PM (50 minutes)

We study the problem of propagation of an input electromagnetic pulse through a long two-level laser amplifier under trivial initial conditions. We consider an unstable model described by the Maxwell–Bloch equations without spectral broadening. We obtain rigorous asymptotic results at large times, in two regions: in a region near the light cone and in the tail region. The region near the light cone is described by pulses of narrowing width and growing amplitude, while in the tail region, a new type of solitons is found against an oscillating background.

Primary authors: MINAKOV, Oleksandr (Charles University); KOTLYAROV, Volodymyr

Presenter: MINAKOV, Oleksandr (Charles University)

Contribution ID: 12

Type: **Lecture**

Generalized Hydrodynamics for the Volterra lattice

Thursday, June 6, 2024 2:30 PM (50 minutes)

Despite needing a complete mathematical foundation, the theory of Generalized Hydrodynamics has been used to obtain precise approximations of the correlation functions for several integrable models. For example, H. Spohn used this theory to compute the correlation function of the Toda lattice.

We consider another integrable model, namely the Volterra lattice. We introduce the Generalized Gibbs Ensemble for this lattice and relate it to the Anti-symmetric β ensemble, a classical random matrix model for anti-symmetric matrices. This connection allows us to explicitly compute the density of states for the Volterra lattice in terms of the random matrix ensemble one. Given this density, we can apply the theory of GHD to obtain a linear approximation of the correlation function for our model.

This talk is mainly based on the following paper:

- G. M., \textit{Generalized Hydrodynamics for the Volterra lattice: ballistic and nonballistic behavior of correlation functions.} arXiv preprint: 2404.08499

Primary author: MAZZUCA, Guido (Tulane University)

Presenter: MAZZUCA, Guido (Tulane University)

Contribution ID: 16

Type: **Lecture**

Biorthogonal measures, polymer partition functions, and random matrices.

Tuesday, June 4, 2024 11:00 AM (50 minutes)

In this talk, I will describe a particular class of biorthogonal measures related to discrete and semi-discrete polymers (Log-Gamma, O'Connell-Yor, and mixed). More precisely, I will show that the Laplace transform of the partition function of the mentioned polymers coincides with the multiplicative statistics of these biorthogonal measures. This result can be seen as a finite N variant of the connection between the narrow wedge solution of the KPZ equation and the Airy point process. It generalizes previous results of Imamura and Sasamoto for the (homogeneous) O'Connell-Yor polymer. Time permitting, I will show some applications to the small-temperature limit of these polymers and their relation with matrix models. These results have been obtained jointly with Tom Claeys.

Primary author: CAFASSO, Mattia

Presenter: CAFASSO, Mattia

Contribution ID: 17

Type: **Lecture**

Quantum intersection numbers on the moduli space of curves and the Gromov-Witten invariants of the projective line

Wednesday, June 5, 2024 9:10 AM (50 minutes)

I will talk about our recent joint work with Xavier Blot, where we related the quantum intersection numbers on the moduli space of curves to the stationary relative Gromov-Witten invariants of the projective line with an insertion of a Hodge class.

As a corollary, this gives a new geometric interpretation of the standard intersection numbers of psi-classes on the moduli space of curves. We also give a new, much shorter proof, of an explicit formula for the “purely quantum” intersection numbers, which was obtained before by Xavier Blot, and which relates these numbers of the one-part double Hurwitz numbers.

Primary author: BURYAK, Alexandr (HSE Moscow & Skoltech)

Presenter: BURYAK, Alexandr (HSE Moscow & Skoltech)

Contribution ID: 18

Type: **Lecture**

The extended Ablowitz-Ladik hierarchy and a generalized Frobenius manifold

We define a certain extension of the Ablowitz-Ladik hierarchy, and show that it possesses a tau structure and Virasoro symmetries. We prove that this integrable hierarchy coincides with the topological deformation of the Principal Hierarchy of a generalized Frobenius manifold with non-flat unity.

Primary author: ZHANG, Youjin (Tsinghua University)

Presenter: ZHANG, Youjin (Tsinghua University)

Contribution ID: 19

Type: **Lecture**

Affine Gaudin Bethe Ansatz and the ODE/IM correspondence

Monday, June 3, 2024 11:00 AM (50 minutes)

We consider the monodromy-free opers corresponding to solutions of the Affine Gaudin Bethe Ansatz equations.

We define and study the spectral determinants (called Q functions) for these opers. We conjecture that the Q-functions obtained from the Affine Gaudin Bethe Ansatz coincide with the Q-functions of the Bazhanov-Lukyanov-Zamolodchikov opers with the monster potential, which are related to the quantum KdV flows according to the ODE/IM correspondence. We give supporting evidence for this conjecture.

Primary author: MASOERO, Davide (Lisbon University)

Presenter: MASOERO, Davide (Lisbon University)

Contribution ID: 24

Type: **Lecture**

Discrete Painlevé equations in random partitions and planar maps

Tuesday, June 4, 2024 9:30 AM (50 minutes)

The aim of this talk is to explain the connections between the discrete Painlevé I-II equations and certain random and combinatoric models. In the first part of the talk, we will start from a classical result by Borodin, which allows us to calculate the probability distributions of the first parts of random partitions with Poissonized Plancherel measure via a recurrence relation using solutions of the discrete Painlevé II equation. Then, we will see a generalization of this result, that we proved with T. Chouteau, in the case of the so-called “multicritical” Schur measures. In the second part, we will discuss instead the appearance of the discrete Painlevé I equation in the context of counting problems for planar quadrangulation with given geodesic distance and how to explain it from an orthogonal polynomials perspective (work in progress with J. Bouttier).

Primary author: TARRICONE, Sofia (IPhT, CEA Paris-Saclay)

Presenter: TARRICONE, Sofia (IPhT, CEA Paris-Saclay)

Contribution ID: 25

Type: **Lecture**

On Dubrovin-Novikov brackets

Monday, June 3, 2024 9:30 AM (50 minutes)

Dubrovin and Novikov initiated the study of local homogeneous differential-geometric Poisson brackets of arbitrary degree k in their seminal 1984 paper. Despite several results in low degree, very little is known about their structure for arbitrary k . After an introduction to the topic we report on our recent results on the structure of DN brackets of degree k . We show that certain linear combinations of the coefficients of a DN bracket define k connections which are all flat and that the Poisson cohomology of a DN bracket is related with the Chevalley-Eilenberg cohomology of a Lie algebra which is naturally associated with the bracket. Joint work with M. Casati.

Primary author: CARLET, Guido (Université de Bourgogne)

Presenter: CARLET, Guido (Université de Bourgogne)

Contribution ID: 26

Type: **not specified**

Quasimodular functions from Donaldson-Thomas invariants

Wednesday, June 5, 2024 11:00 AM (50 minutes)

In this talk, I will explain how to construct quasimodular forms from Betti numbers of moduli spaces of one-dimensional coherent sheaves on the projective plane. This gives a proof of some predictions from theoretical physics about the refined topological string theory in the Nekrasov-Shatashvili limit. The proof of this result combines various tools of modern enumerative algebraic geometry, such as derived categories, Gromov-Witten invariants, and tropical geometry. This work is in part joint with Honglu Fan, Shuai Guo, and Longting Wu.

Presenter: BOUSSEAU, Pierrick (University of Georgia)

Contribution ID: 27

Type: **Lecture**

Borel multi-transforms, and quantum differential equations of P^1 -bundles

Monday, June 3, 2024 3:20 PM (50 minutes)

The qDEs define a class of ordinary differential equations in the complex domain, whose study represents a challenging and active area in both contemporary geometry and mathematical physics. The qDEs define rich invariants attached to smooth projective varieties. These equations encapsulate information not only about the enumerative geometry of varieties but also, conjecturally, about their topology and complex geometry. The way to disclose such a huge amount of data is through the study of the asymptotics and monodromy of their solutions.

In this talk, the speaker will address the problem of explicitly integrating the quantum differential equations of varieties and will report on his progress in a long-term project on this topic. Focusing on the case of projectivizations of vector bundles, he will first introduce a family of integral transforms and special functions (the integral kernels). Then, he will show how to use these tools to find explicit integral representations of solutions. Based on arXiv:2005.08262 (Memoirs of the EMS, 2022) and arXiv:2210.05445 (Journal Math. Pures et Appl. 2024).

Primary author: COTTI, Giordano (Universidade de Lisboa, Portugal)

Presenter: COTTI, Giordano (Universidade de Lisboa, Portugal)

Contribution ID: 28

Type: **Lecture**

Quantum KdV, quasimodular forms, and shifted symmetric functions

Monday, June 3, 2024 2:30 PM (50 minutes)

I will review recent progress in the study of the spectrum of the quantum double ramification hierarchy associated with the trivial cohomological field theory, i.e., of the quantum KdV hierarchy in its first Poisson structure. A remarkable relation to quasimodular forms naturally suggests a conjecture for the expansion to all orders of the spectrum, and we verify the conjecture explicitly at first order. Based on joint work with Jan-Willem van Ittersum and work in progress with Jan-Willem van Ittersum and Don Zagier.

Primary author: RUZZA, Giulio (Universidade de Lisboa)

Presenter: RUZZA, Giulio (Universidade de Lisboa)

Contribution ID: 29

Type: **Lecture**

The extended Ablowitz-Ladik hierarchy and a generalized Frobenius manifold

Wednesday, June 5, 2024 11:50 AM (50 minutes)

We define a certain extension of the Ablowitz-Ladik hierarchy, and show that it possesses a tau structure and Virasoro symmetries. We prove that this integrable hierarchy coincides with the topological deformation of the Principal Hierarchy of a generalized Frobenius manifold with non-flat unity.

Presenter: Prof. ZHANG, Youjin

Contribution ID: 30

Type: **Lecture**

Resurgent large genus asymptotics of intersection numbers

Monday, June 3, 2024 11:50 AM (50 minutes)

I will present a new approach to the computation of the large genus asymptotics of intersection numbers, in particular of Witten—Kontsevich, Theta and r-spin intersection numbers. Our technique is based on a resurgent analysis of the generating series of such intersection numbers, and relies on the presence of a quantum curve and the determinant formulae. With this approach, we are able to extend the recent results of Aggarwal with the computation of subleading corrections, solving a conjecture of Guo–Yang and initiating the development of a universal technique to explore large order asymptotics of enumerative problems that appear in the context of topological recursion. Based on joint work with B. Eynard, A. Giacchetto, P. Gregori and D. Lewański.

Primary author: GARCIA-FAILDE, Elba (Universitaire de Jussieu)

Presenter: GARCIA-FAILDE, Elba (Universitaire de Jussieu)

Contribution ID: 31

Type: **Lecture**

Large deviations for the log-Gamma polymer

Thursday, June 6, 2024 9:30 AM (50 minutes)

I will present a conjecture about large deviations of the partition function of the log-Gamma polymer. We can rigorously prove our result, except for one step for which we only have heuristic evidence. I will show that the conjectured large deviation rate function matches with that of last passage percolation with exponential weights in the zero-temperature limit, and with the lower tail of the Tracy-Widom distribution for moderate deviations.

The talk will be based on joint work with Julian Mauersberger.

Primary author: CLAEYS, Tom (UCLouvain)

Presenter: CLAEYS, Tom (UCLouvain)

Contribution ID: 32

Type: **Lecture**

Confinement effects in fluid-boundary interactions

Thursday, June 6, 2024 4:00 PM (50 minutes)

Hydrodynamics has motivated many of the advances that lie at the foundations of the mathematics of completely integrable models; the interplay between a fluid and its boundaries adds to the richness, both from a mathematical and a physical perspective, of phenomena that can arise in this area. This talk will present examples of how boundary effects lead to notable outcomes. These effects can be analytically predicted by simple mathematical models (and their integrability), and observed in “simple” experimental setups.

Primary author: CAMASSA, Roberto (Chapel Hill)

Presenter: CAMASSA, Roberto (Chapel Hill)

Contribution ID: 33

Type: **Lecture**

Classical W-algebras and generalized Drinfeld-Sokolov hierarchies

Friday, June 7, 2024 9:30 AM (50 minutes)

Classical affine W-algebras $W(\mathfrak{g}, O)$ are algebraic structures associated to a simple Lie algebra \mathfrak{g} and a nilpotent orbit O . In this talk we want to review their definition, the construction (for all but seven nilpotent orbits for exceptional Lie algebras) of an integrable hierarchy of PDEs known as generalized Drinfeld-Sokolov hierarchy and how to derive the tau-structure of the hierarchy.

Primary author: VALERI, Daniele (Roma III)

Presenter: VALERI, Daniele (Roma III)