

The IR limit of Hořava Gravity

Mario Herrero-Valea
SISSA, INFN & IFPU

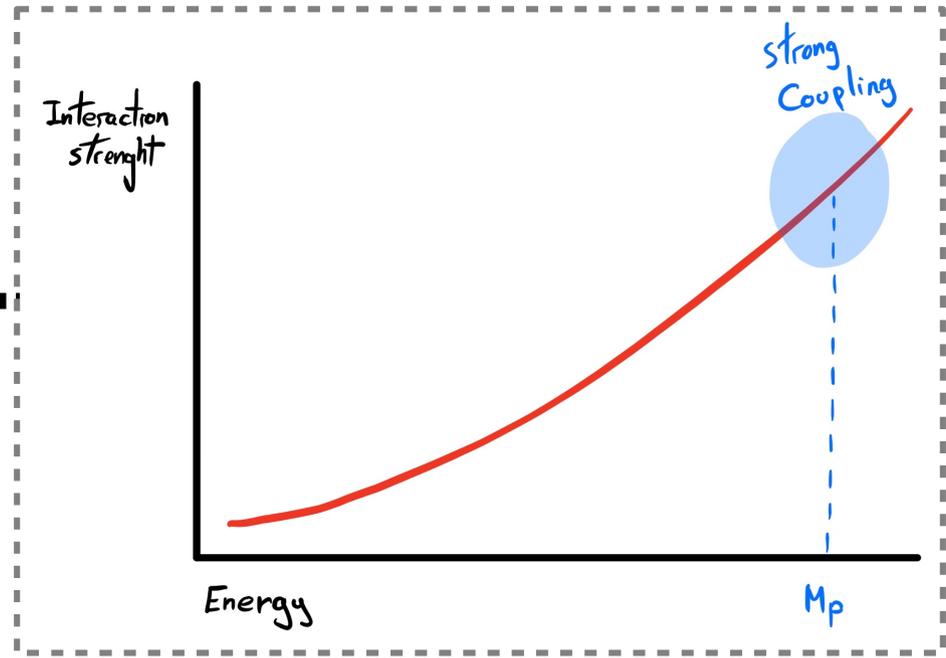
ArXiv:1512.02250, 1706.06809, 1905.03798, w.i.p.
With: A. Barvinsky, D. Blas, L. Obradovic, S. Sibiryakov
and C. Steinwachs

**Why we are not
happy with GR?**

**It does not extend to
arbitrary high energies**

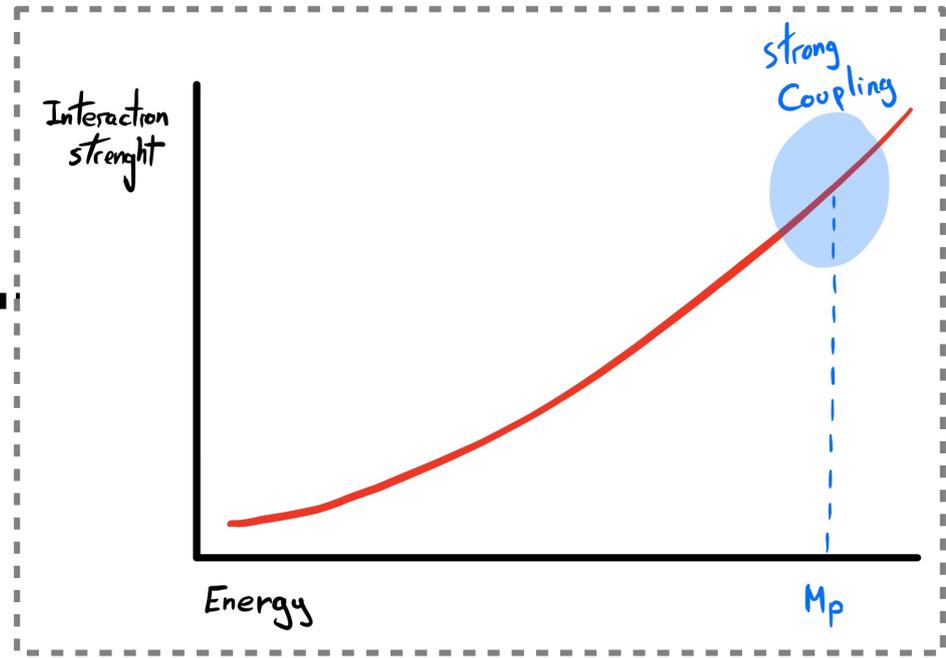
**It lacks an explanation
for observed
gravitational phenomena**

Why we are not happy with GR?



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Dark Matter

Dark Energy

So what can we do?

Add new degrees of freedom

Modify the interactions

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Hordensky, Beyond
Hordensky, Dhost

String theory

Massive gravity

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However, Lorentz
invariance is **very**
constraining

Ghosts, lost of unitarity...

So what can we do?

Add new degrees of freedom

Hordensky, Beyond
Hordensky, Dhost

String theory

Massive gravity

Modify the interactions

Quadratic Gravity

Stelle, 1977

Fradkin & Tseytlin, 1981

Avramidi and Barvinsky, 1985

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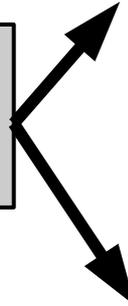
We abandon Lorentz invariance *at high energies*

This evades
pathologies

No ghosts

No violation
of unitarity

Only a finite number of
interactions is required



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Hořava Gravity

P. Hořava (2009)

Hořava Gravity

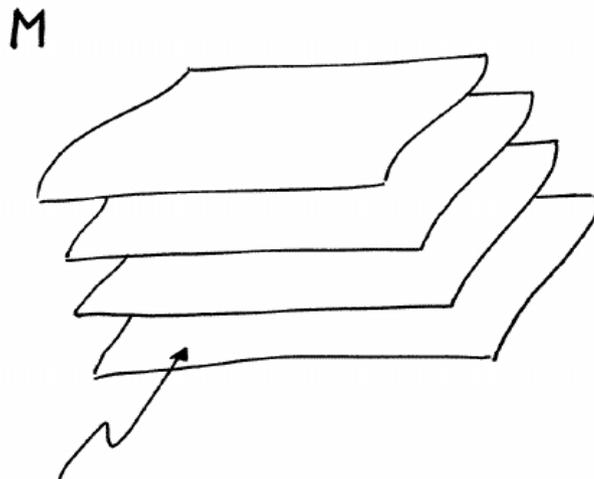
There is a privileged time direction (thus, Lorentz breaking)

The dynamical content is described in terms of ADM

$$ds^2 = N^2 dt^2 - \gamma_{ij} (dx^i + N^i dt)(dx^j + N^j dt)$$

It propagates a TT graviton and *an extra scalar mode*

$$S = \int dt d^d x N \sqrt{\gamma} (K_{ij} K^{ij} - \lambda K^2 - \mathcal{V}(R, \partial_i N))$$



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5 terms in 2+1 dimensions
15 terms in 3+1 dimensions

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Non-projectable HG

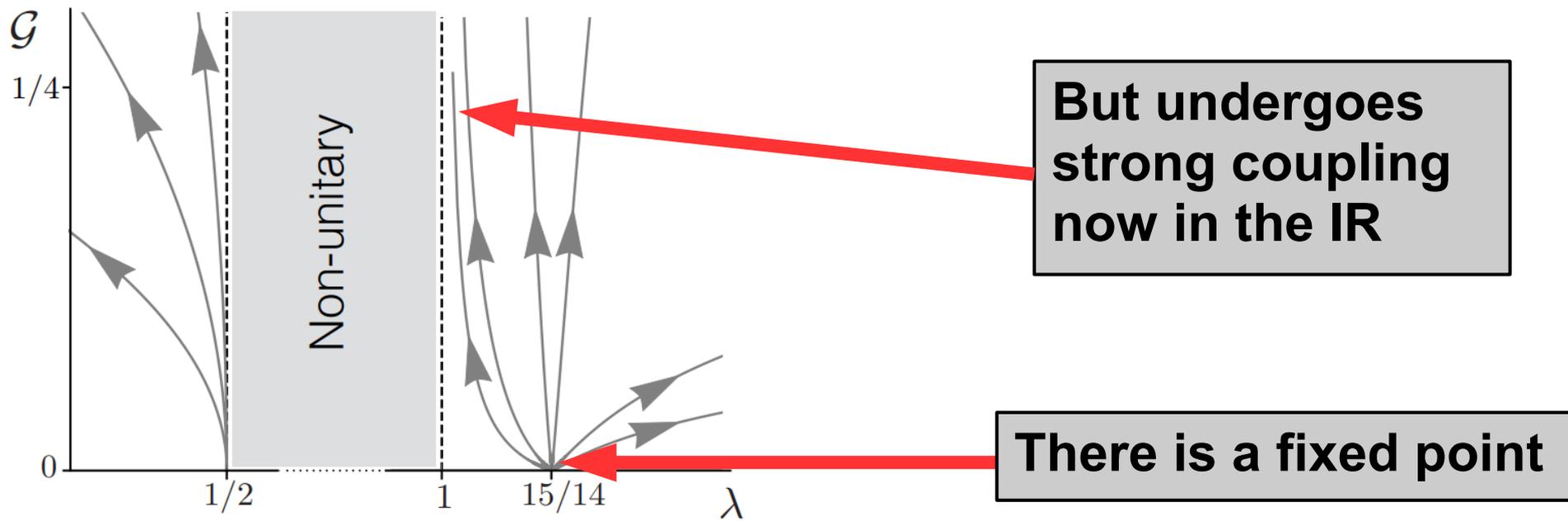
There has been a very extensive study of BHs
Barausse, Liberti, Sotiriou

Problems for QFT:
Global constraint
Instantaneous interaction

Projectable HG

Gauge-fix away the lapse
Avoids the pathologies

QFT well-defined
Bavinsky, Blas, H-V, Sibiryakov, Steinwachs



**But undergoes
strong coupling
now in the IR**

There is a fixed point

Figure from 1706.06809

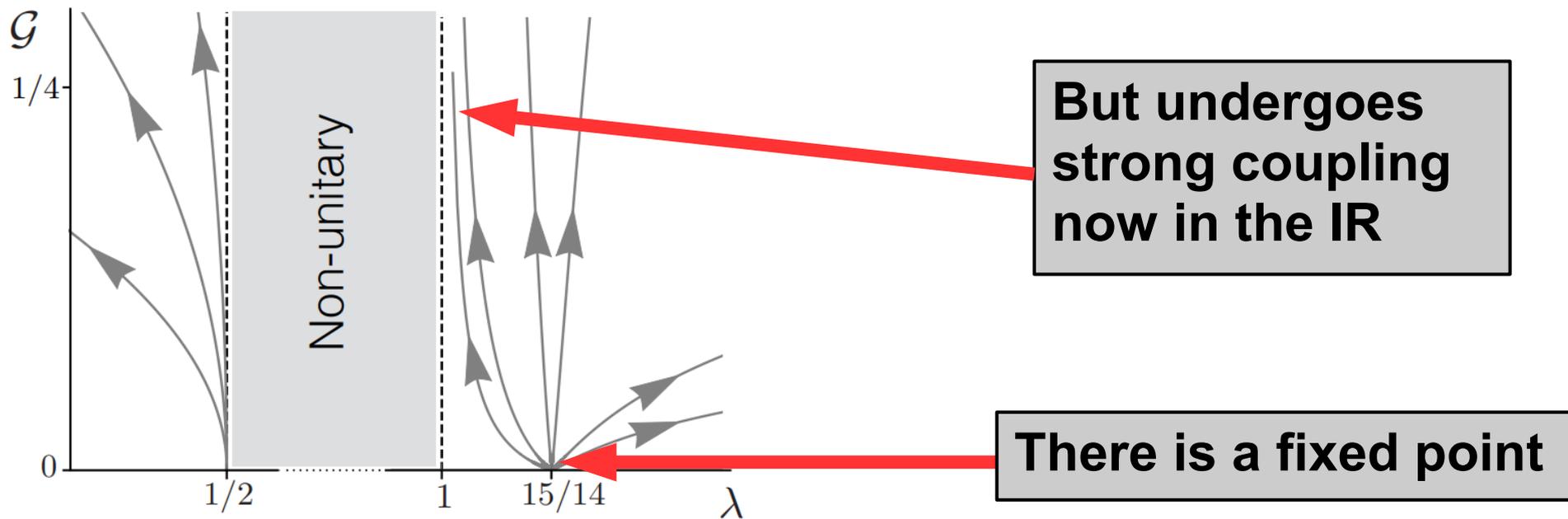


Figure from 1706.06809

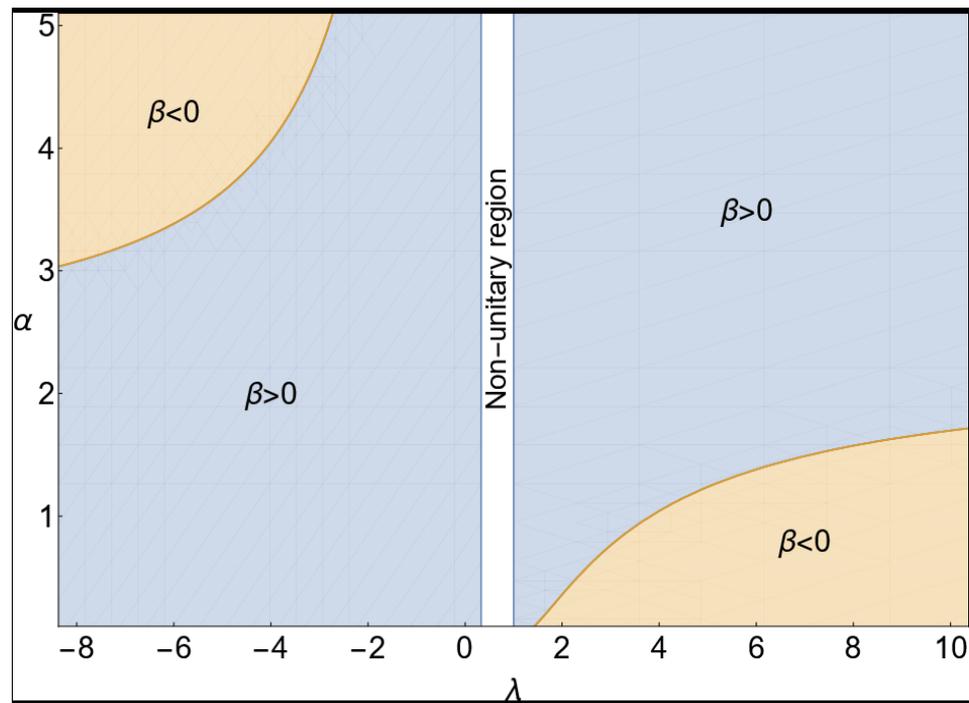


Figure from 1905.03798

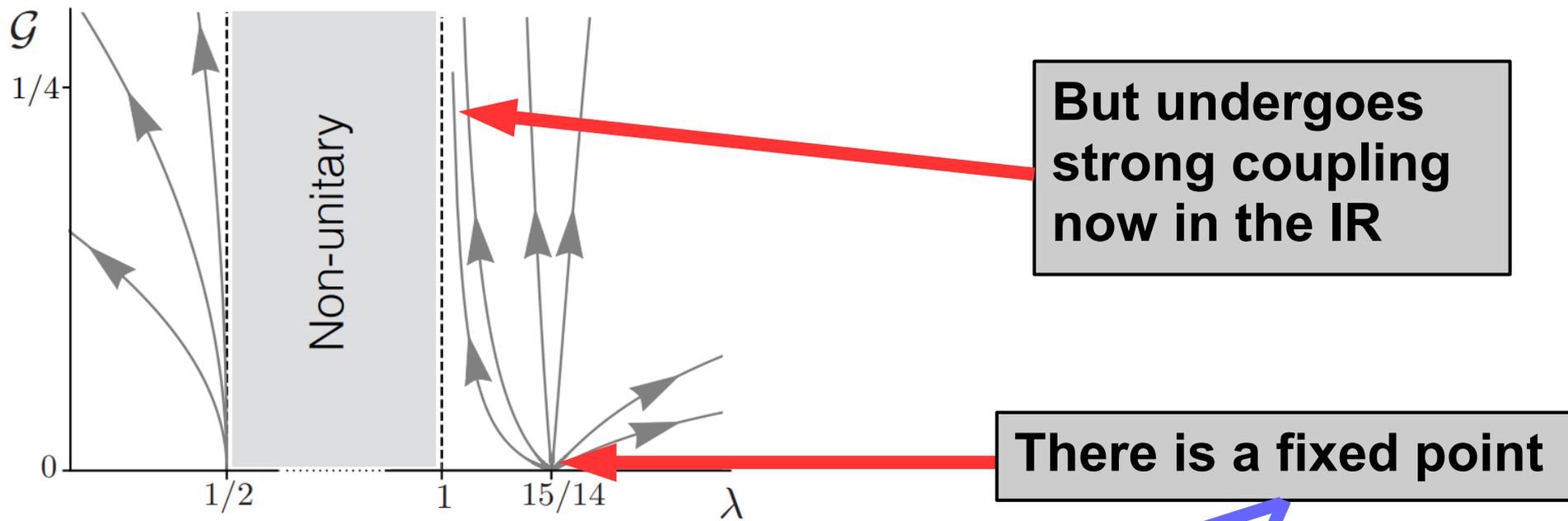
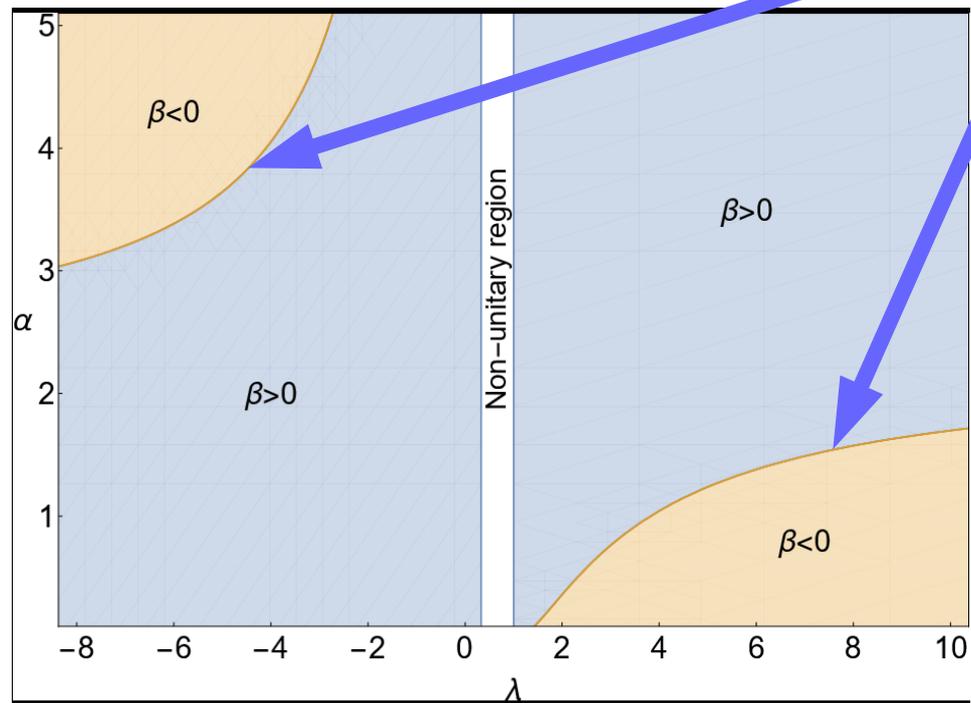


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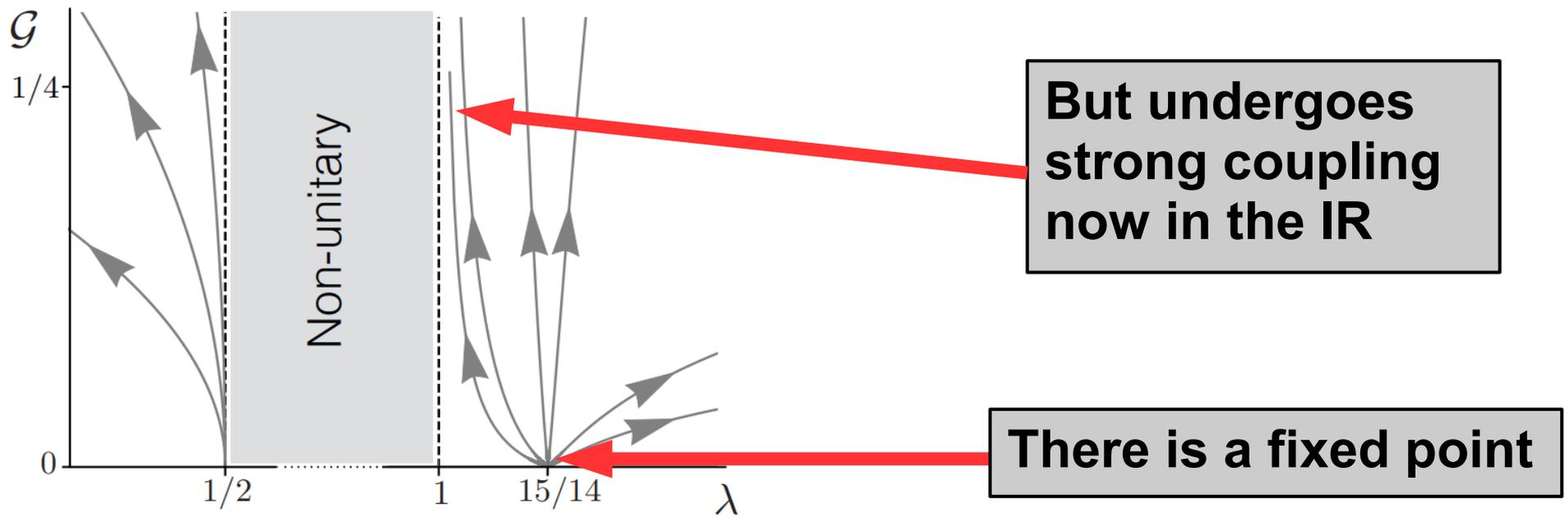


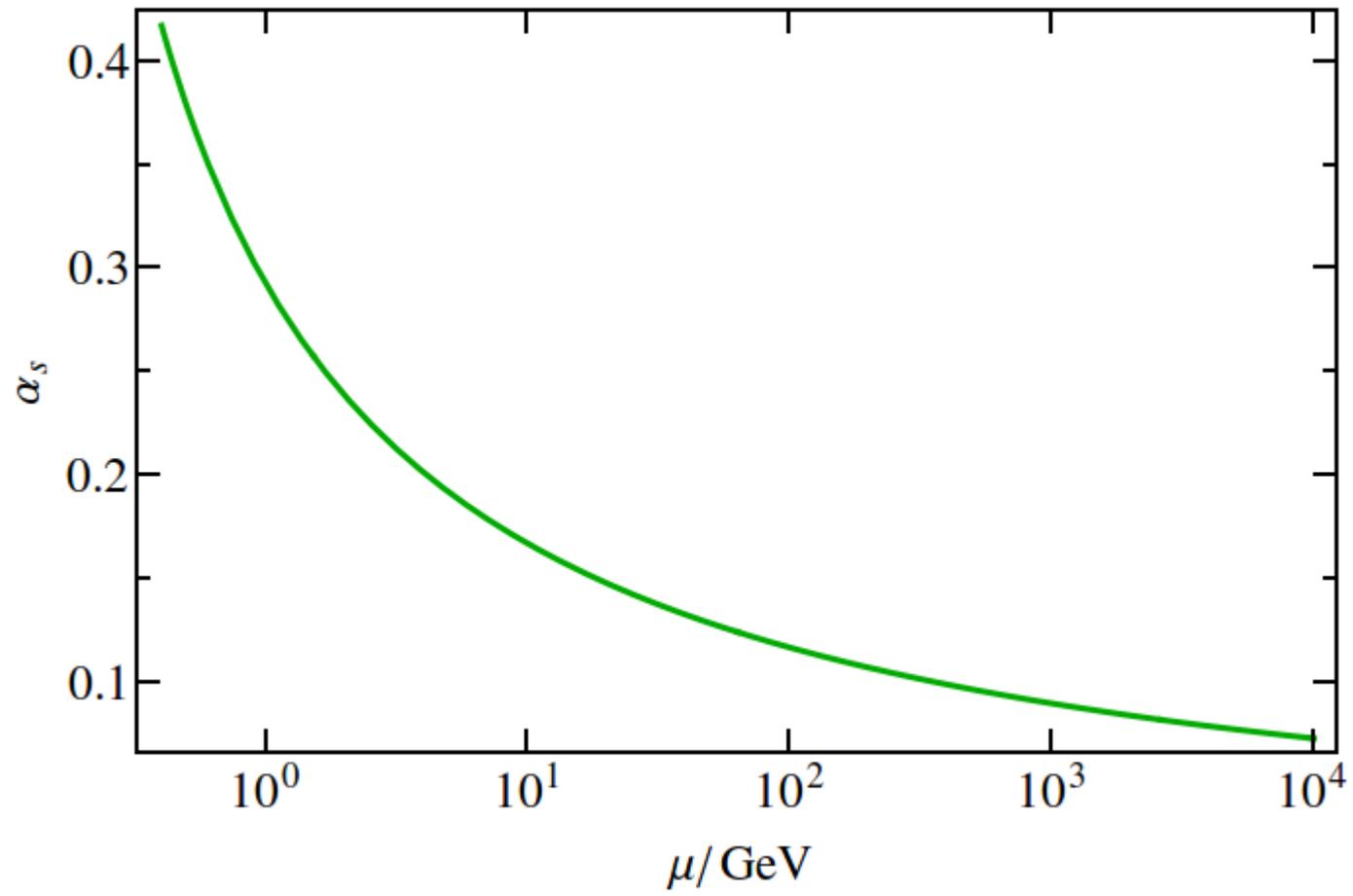
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Phenomenology seems to be doomed

The theory flows in the IR to something which might not be General Relativity.

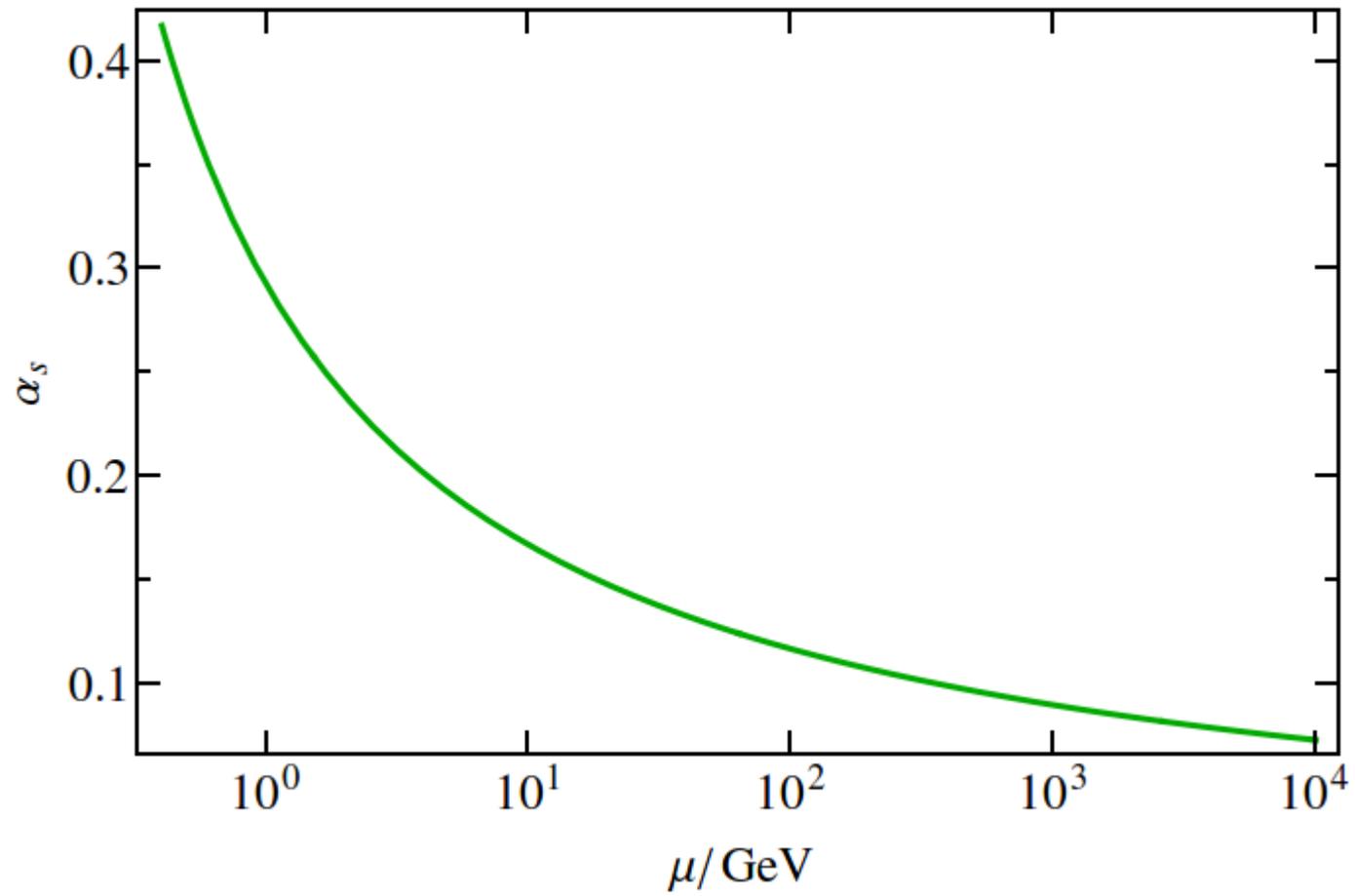
Projectable HG is then just a toy model.





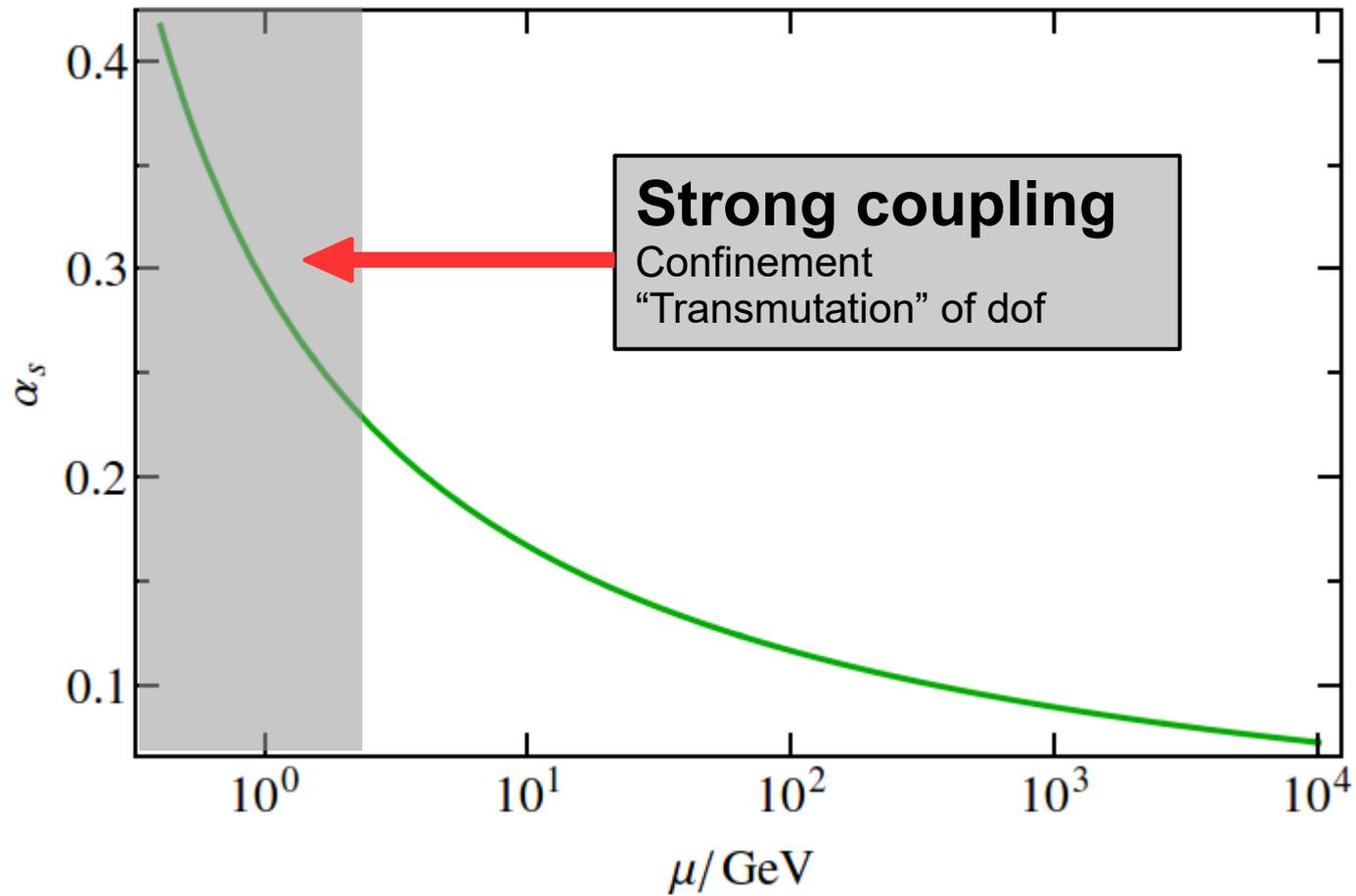
Credit: Wikipedia

QCD



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What if?

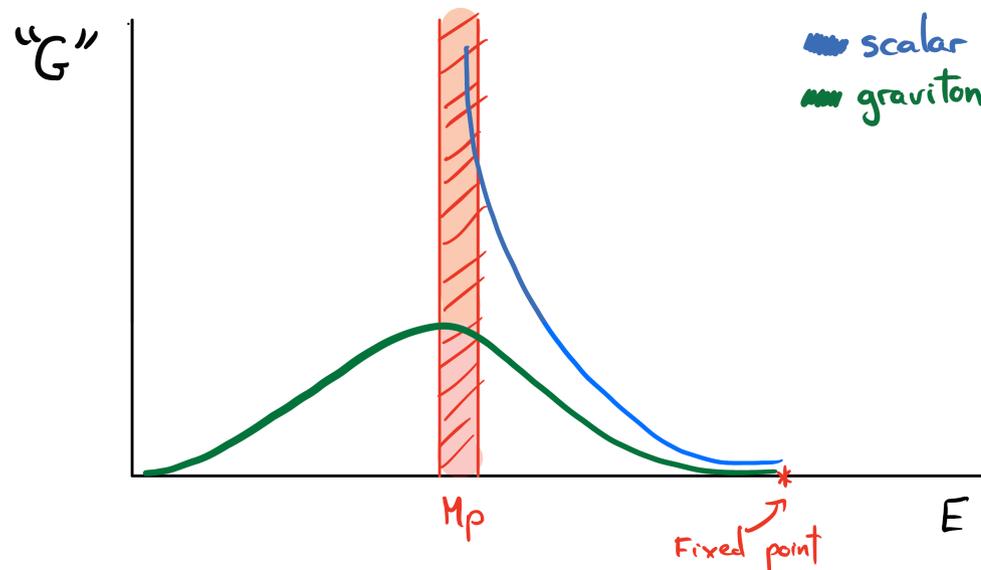
The strong coupling only appears in self-interactions of the scalar mode

Mukohyama (2009)

Gravity mediated interactions of matter always weak

Graviton interactions always weak

The scalar condenses à la QCD -----> Dark Matter



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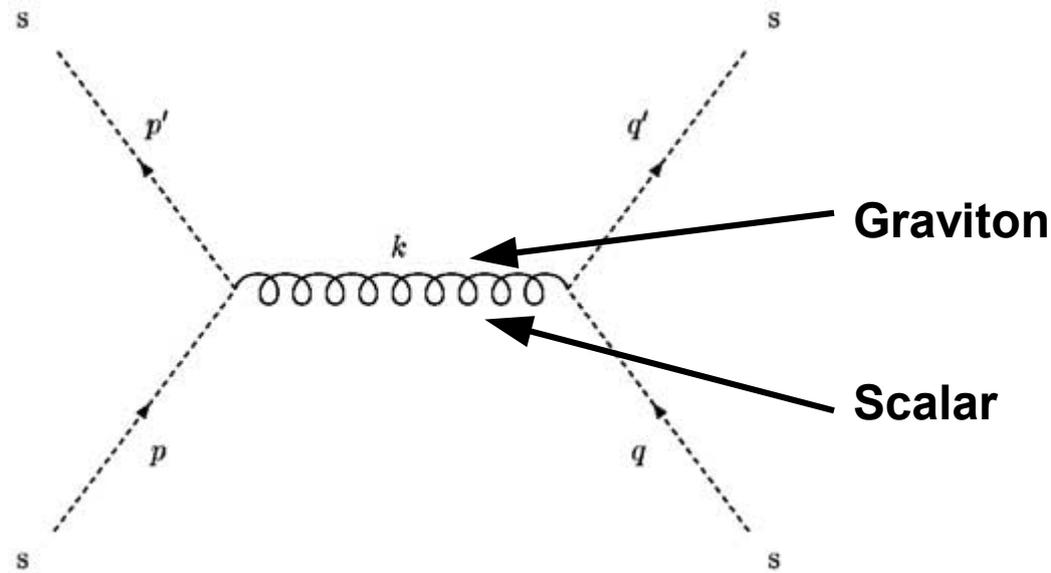
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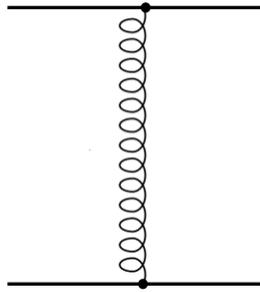
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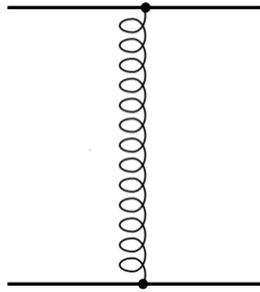
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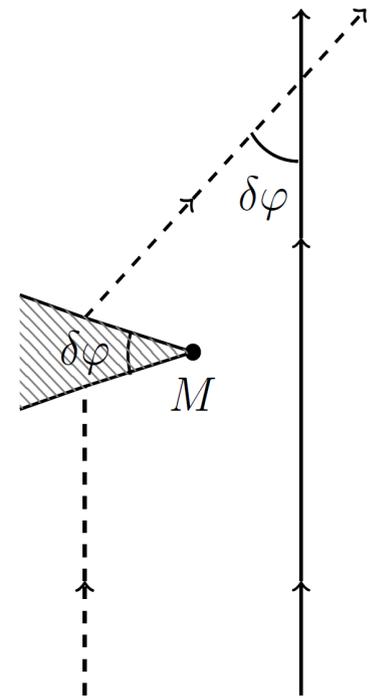


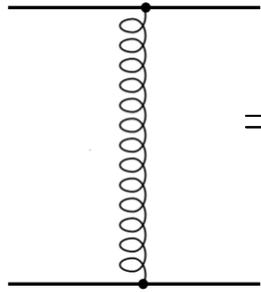
$$= -\frac{8G}{1 - \cos(\theta)} (3m^2 + 2q^2 + (m^2 + 2q^2) \cos(\theta))$$



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***This corresponds to scattering by a conical defect
GR in 2+1 dimensions***

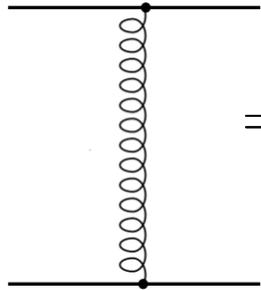




$$= -\frac{128G}{(q^2(1 - \cos(\theta)))} (m^4 + 6m^2q^2 + 4q^4 + 2q^2(m^2 + 2q^2) \cos(\theta))$$

**Which again matches the result of
GR in 3+1**

Note the pole in $q^2=0$!!



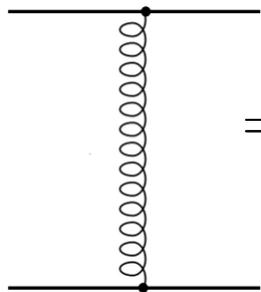
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**We find that interactions by the
scalar mode are always suppressed
when $q \rightarrow 0$ with respect to gravity**

No vDVZ discontinuity



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Conclusions

Hořava Gravity is a proposal for a UV completion of GR

PHG is a bona fide quantum field theory of gravity

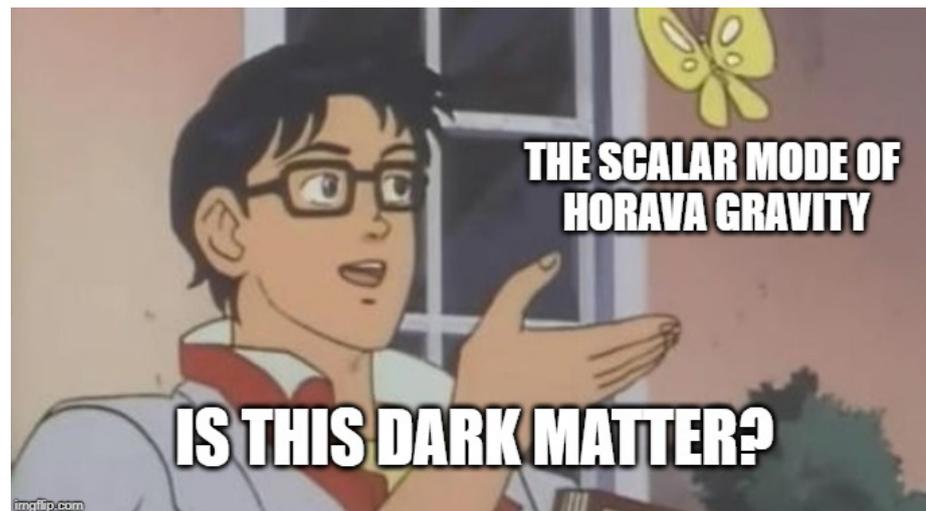
Phenomenology seems problematic but
Strong coupling only in the scalar sector
Matter-gravity sector is always weakly coupled

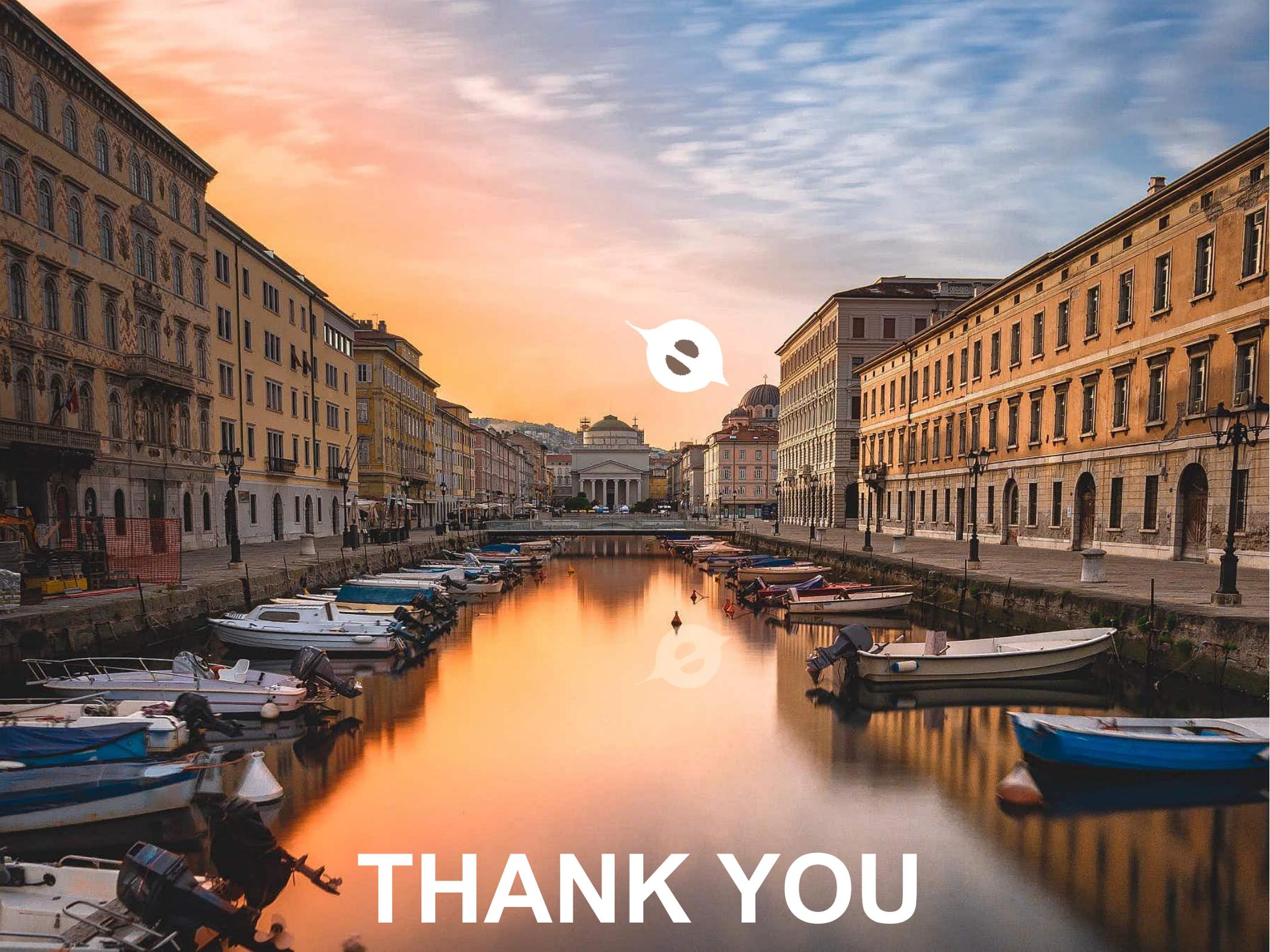
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THANK YOU