

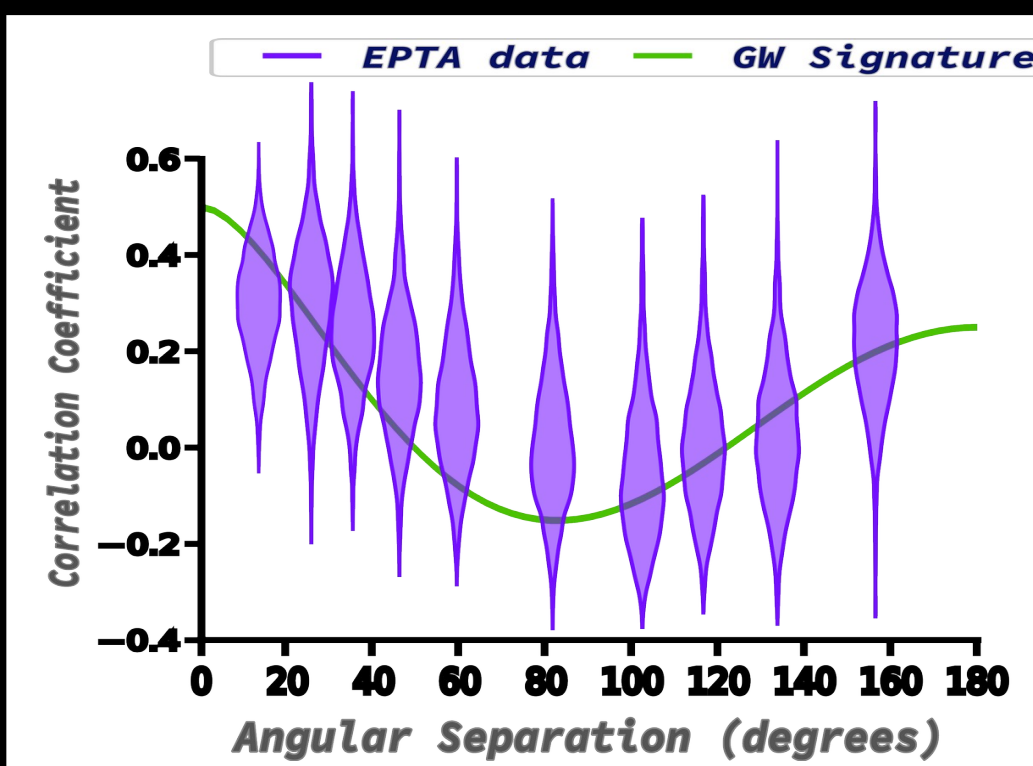
Implications of GW searches in the EPTA DR2

arXiv:230616227

Alberto Sesana
(University of Milano-Bicocca)

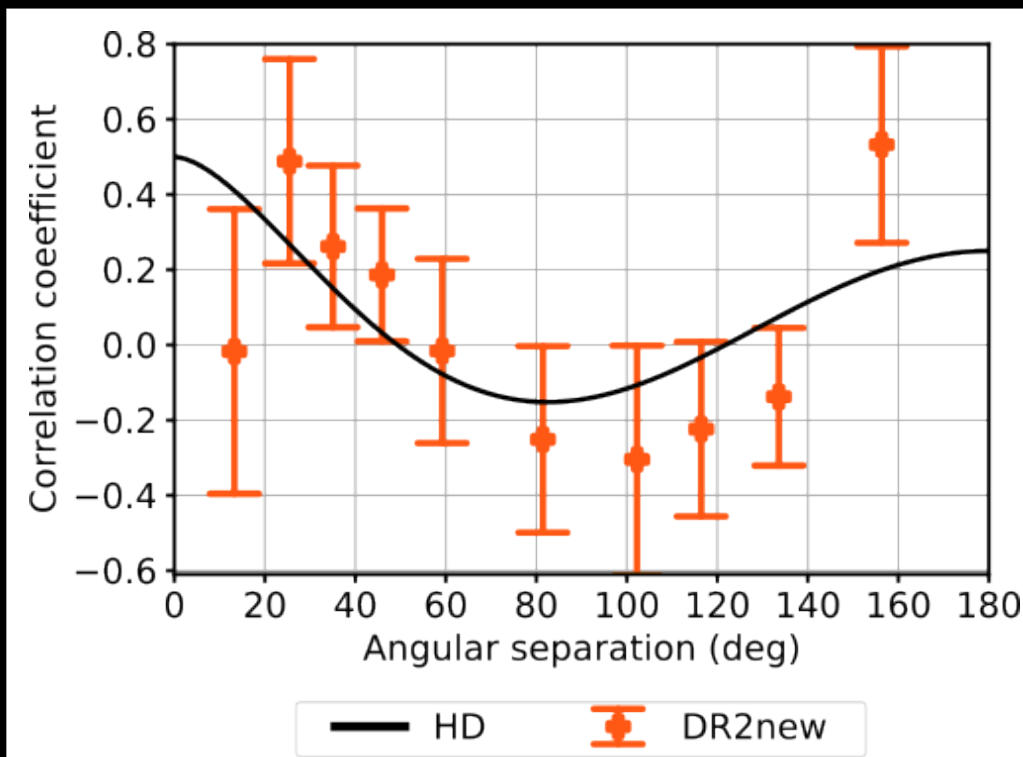
-for the European (+Indian) Pulsar Timing Array-





Bayesian analysis

ID	Model	DR2full1		DR2full+	DR2new		DR2new+
		ENTERPRISE	FORTYTWO	ENTERPRISE	ENTERPRISE	FORTYTWO	ENTERPRISE
1	PSRN + CURN	–	–	–	–	–	–
2	PSRN + GWB	4	5	4	60	62	65
3	PSRN + CLK	< 0.01	< 0.01	< 0.01	0.2	1.2	0.3
4	PSRN + EPH	< 0.01	$\sim 10^{-4}$	< 0.01	0.2	0.2	1.3
5	PSRN + CURN + CLK	2	1	2.7	0.8	2	1.6
6	PSRN + CURN + EPH	1	0.1	1	1	1	1.6
7	PSRN + GWB + CURN	3	3	4	27	13	25
8	PSRN + GWB + CLK	5	12	7	28	35	57
9	PSRN + GWB + EPH	3	3	3.6	33	29	43



Frequentist analysis

	DR2full1	DR2full+	DR2new	DR2new+
A_{MP}^2	$4.1^{+5.0}_{-3.9} \times 10^{-31}$	$3.7^{+5.1}_{-4.1} \times 10^{-31}$	$1.5^{+6.7}_{-4.3} \times 10^{-31}$	$4.0^{+7.0}_{-4.6} \times 10^{-31}$
A_{DP}^2	$-1.9^{+4.6}_{-4.1} \times 10^{-31}$	$-0.8^{+5.1}_{-4.3} \times 10^{-31}$	$0.8^{+9.3}_{-5.8} \times 10^{-31}$	$3.9^{+9.1}_{-6.5} \times 10^{-31}$
A_{HD}^2	$2.7^{+3.0}_{-2.5} \times 10^{-30}$	$2.9^{+2.9}_{-2.4} \times 10^{-30}$	$10.0^{+5.1}_{-4.9} \times 10^{-30}$	$11.0^{+4.6}_{-4.4} \times 10^{-30}$
S/N_{MP}	$1.1^{+1.1}_{-1.0}$	$1.0^{+1.1}_{-1.1}$	$0.3^{+1.4}_{-0.9}$	$0.8^{+1.7}_{-1.0}$
S/N_{DP}	$-0.4^{+0.9}_{-0.8}$	$-0.2^{+1.0}_{-0.9}$	$0.1^{+1.5}_{-0.9}$	$0.6^{+1.5}_{-0.9}$
S/N_{HD}	$1.3^{+1.3}_{-1.2}$	$1.4^{+1.2}_{-1.1}$	$3.5^{+2.4}_{-1.7}$	$4.1^{+2.7}_{-1.7}$

**Similar results as
NANOgrav, PPTA, CPTA**

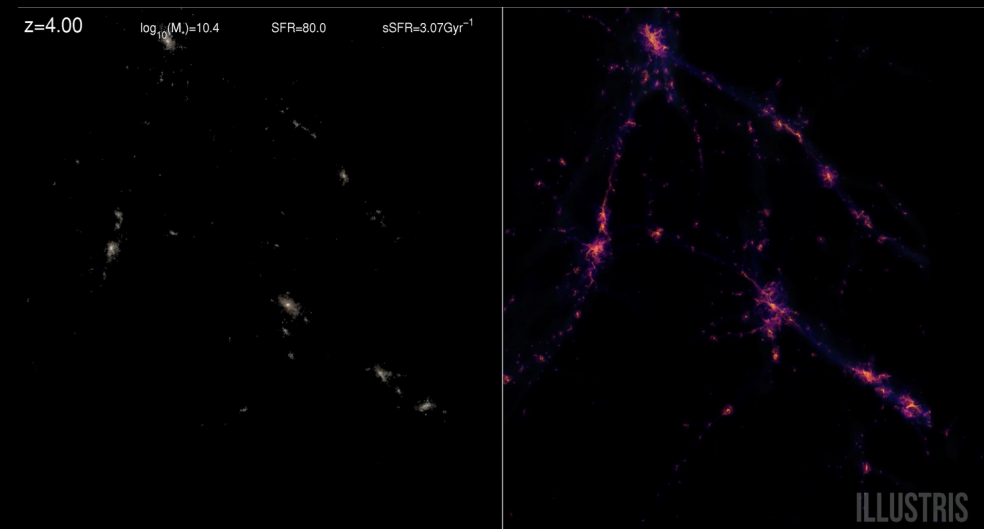
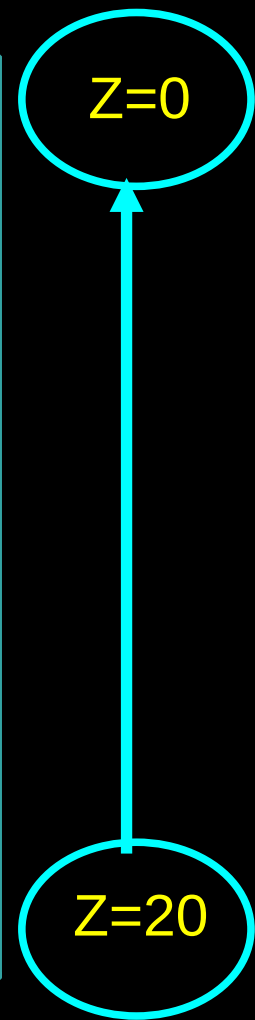
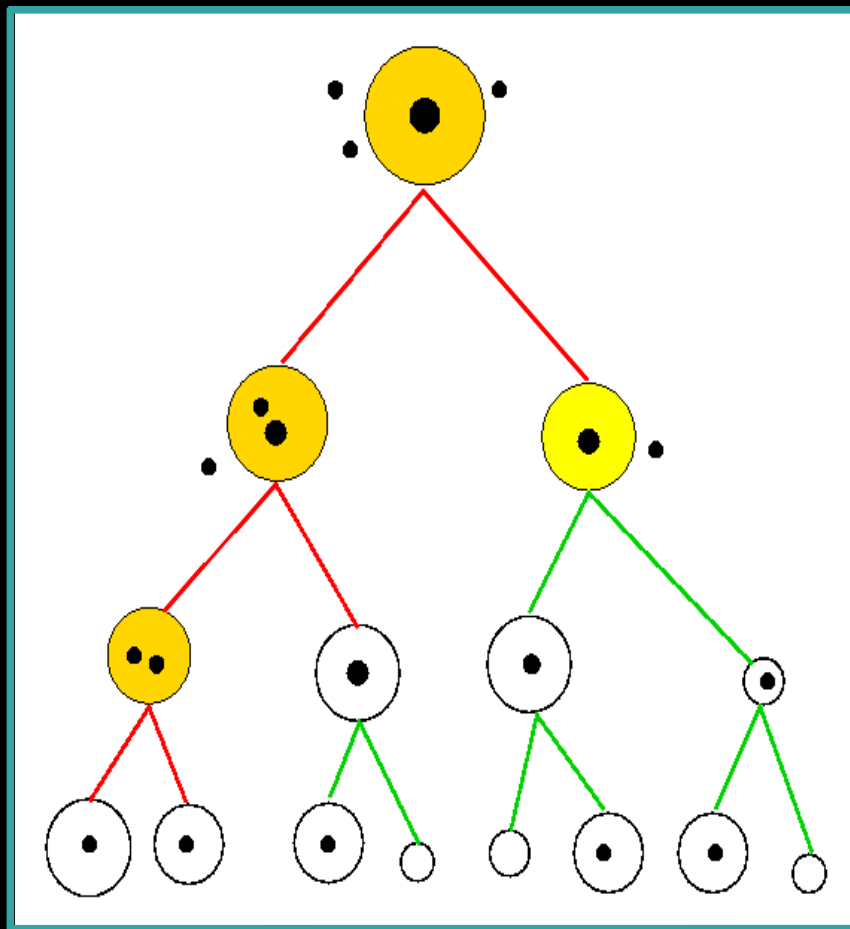
HIERARCHICAL GALAXY & MBH EVOLUTION

GENERAL FRAMEWORK:

Galaxies form hierarchically through a series of mergers and accretion events

Protogalaxies can host seed BH that accrete mass and merge with each other following galaxy mergers

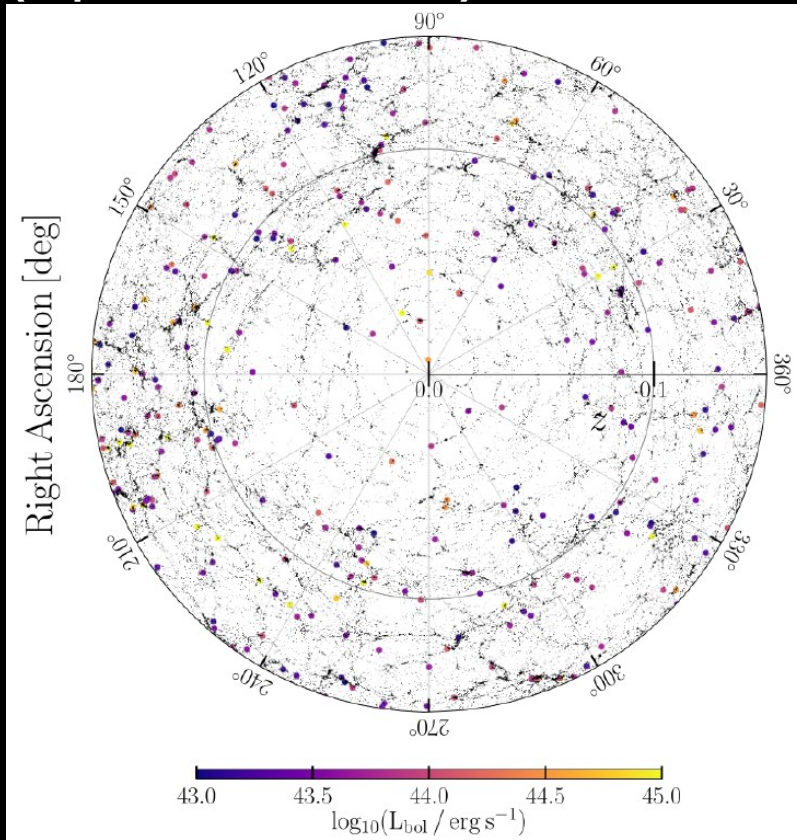
(Volonteri, Haardt & Madau 2003)



(Illustris simulation)

The expected GW signal in the PTA band

(Izquierdo-Villalba+ 22)



The GW characteristic amplitude coming from a population of circular MBH binaries

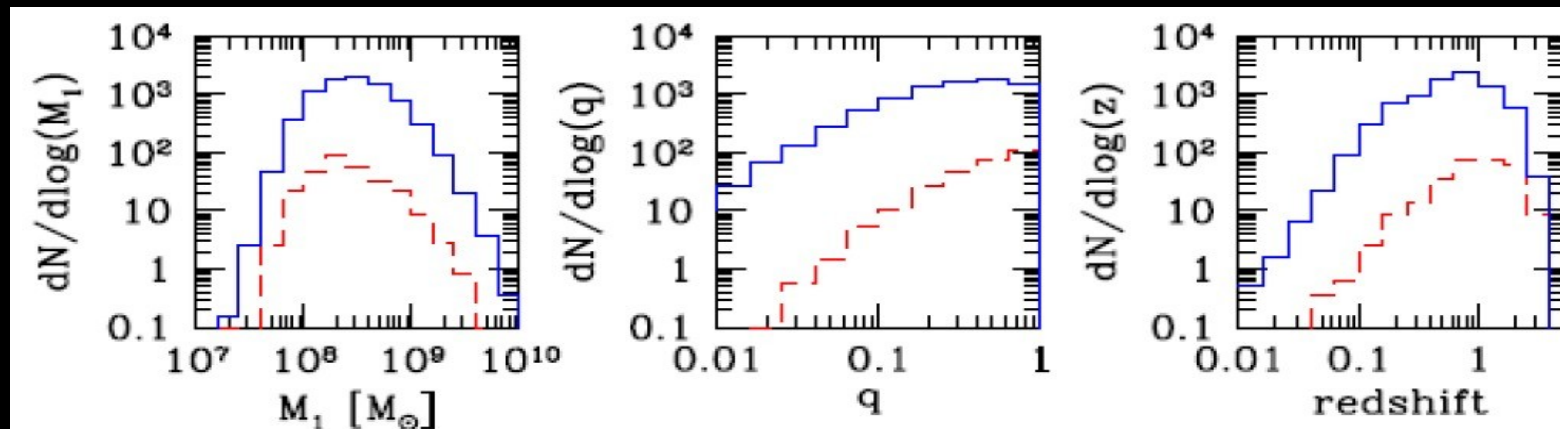
$$h_c^2(f) = \int_0^\infty dz \int_0^\infty d\mathcal{M} \frac{d^3 N}{dz d\mathcal{M} d\ln f_r} h^2(f_r)$$

$$\delta t_{\text{bkg}}(f) \approx h_c(f)/(2\pi f)$$

Theoretical spectrum: simple power law

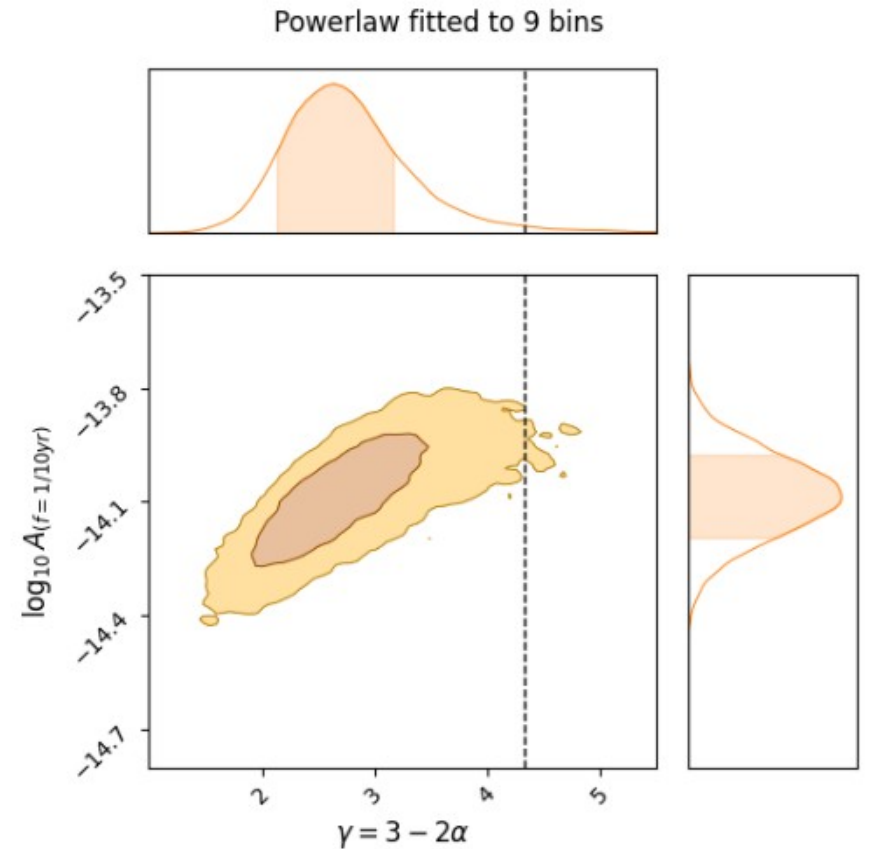
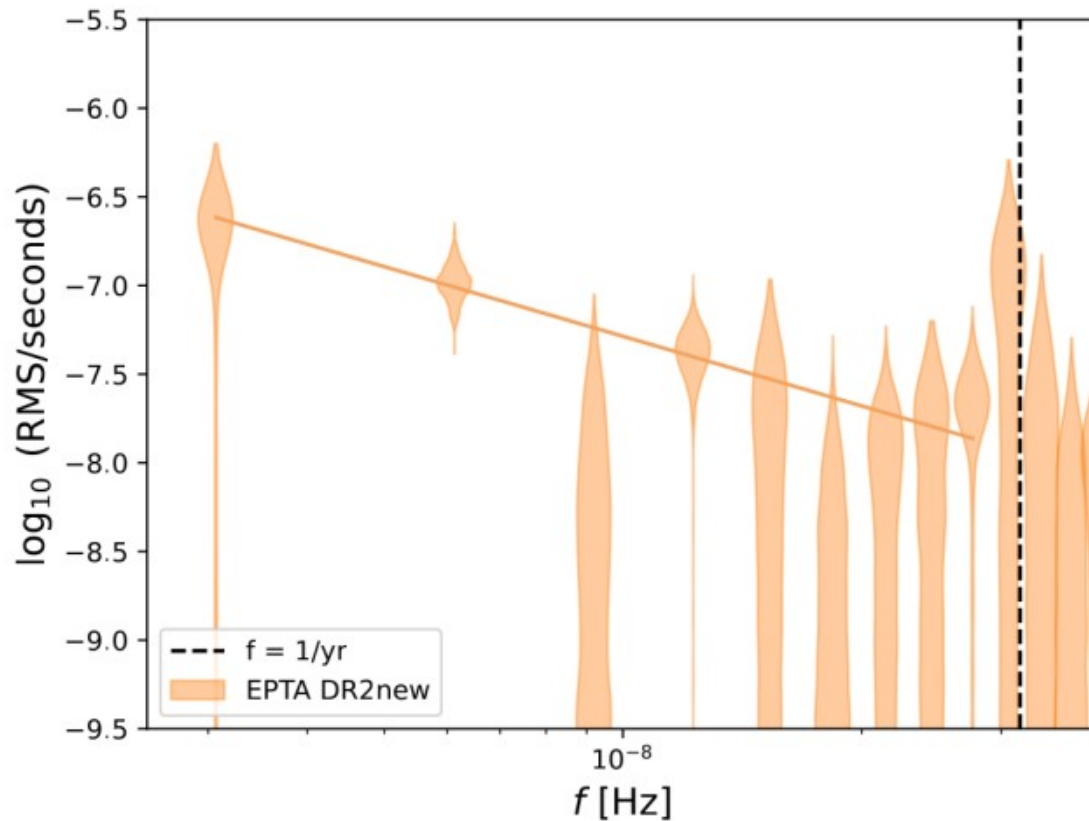
(Phinney 2001)

$$h_c(f) = A \left(\frac{f}{\text{yr}^{-1}} \right)^{-2/3}$$



The signal is contributed by extremely massive ($>10^8 M_\odot$) relatively low redshift ($z < 1$) MBH binaries (AS et al. 2008, 2012)

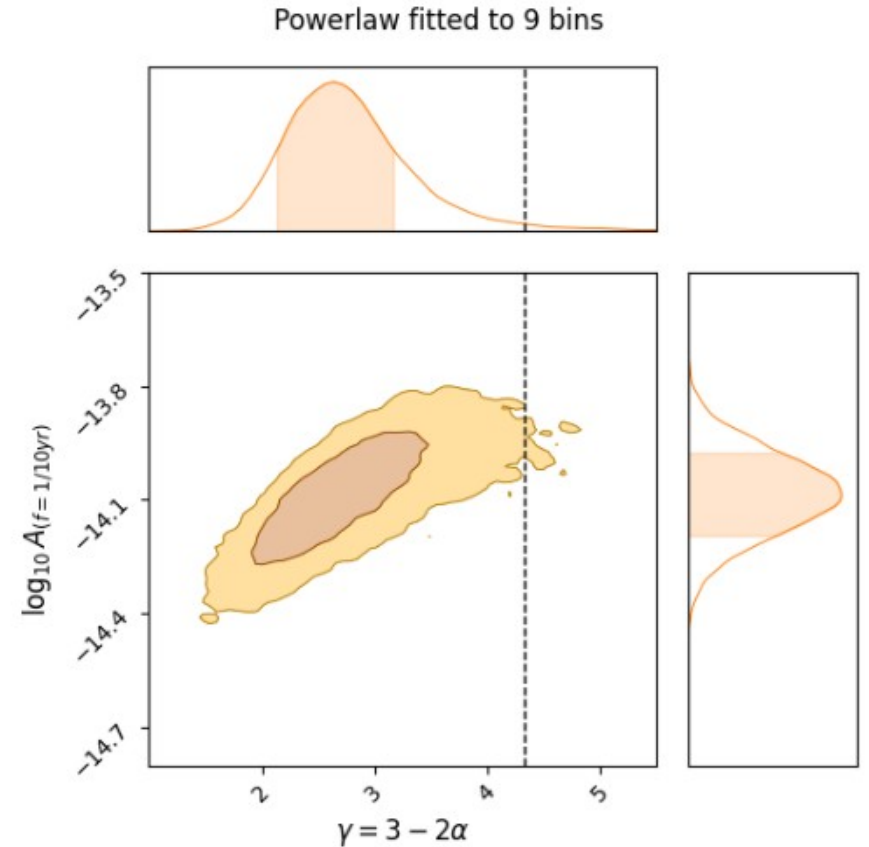
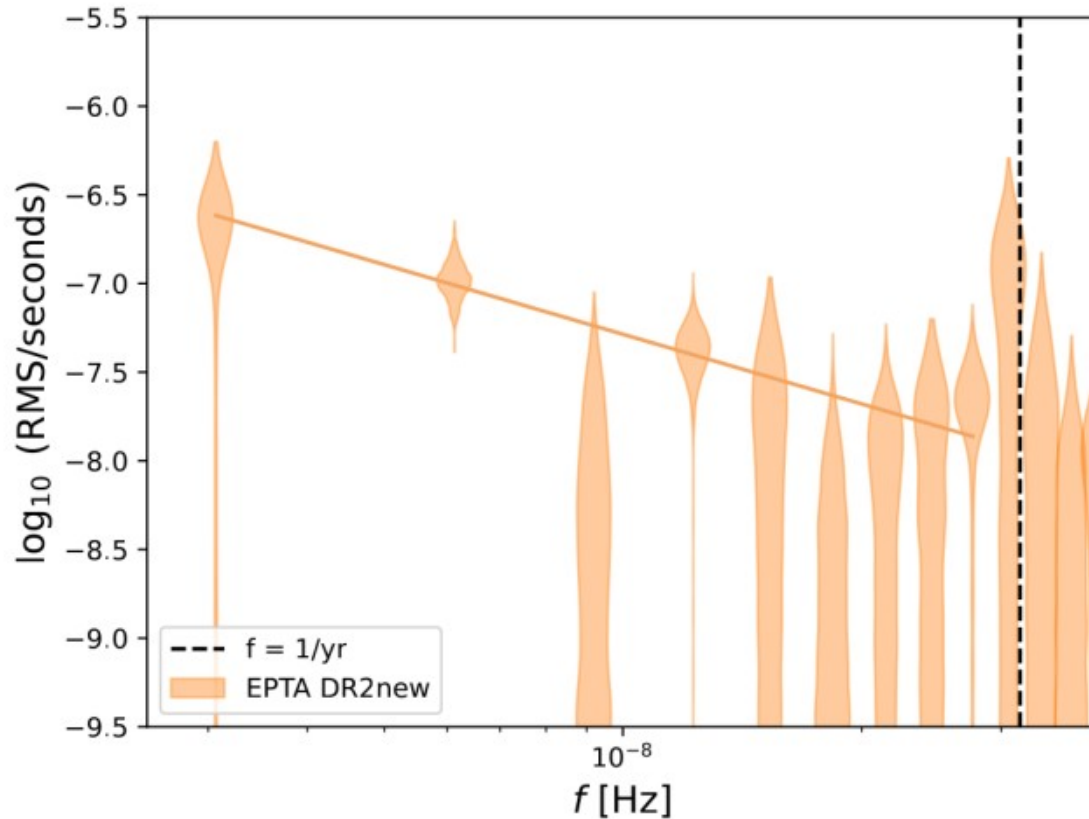
Results of EPTA DR2



- 4 dataset produced: using DR2new here (only new backend)
- HD correlated signal favoured with Bayes factor ~ 60
- power constrained in few bins at low freq
- powerlaw fit: $\gamma \sim 2.7$ $A \sim -14$ [$A(\gamma=13/3) \sim -14.6$]

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THINGS YOU HEAR: “too flat for SMBHBs [add your favorite early Universe model that fits the data]”

“Looking at the arxiv, can't help wondering: is there any early-Universe cosmological process that DOES NOT produce the stochastic gravitational-wave background observed by Pulsar-Timing Arrays?”

Yuri Levin

-It's Inflation!

-It's phase transitions!

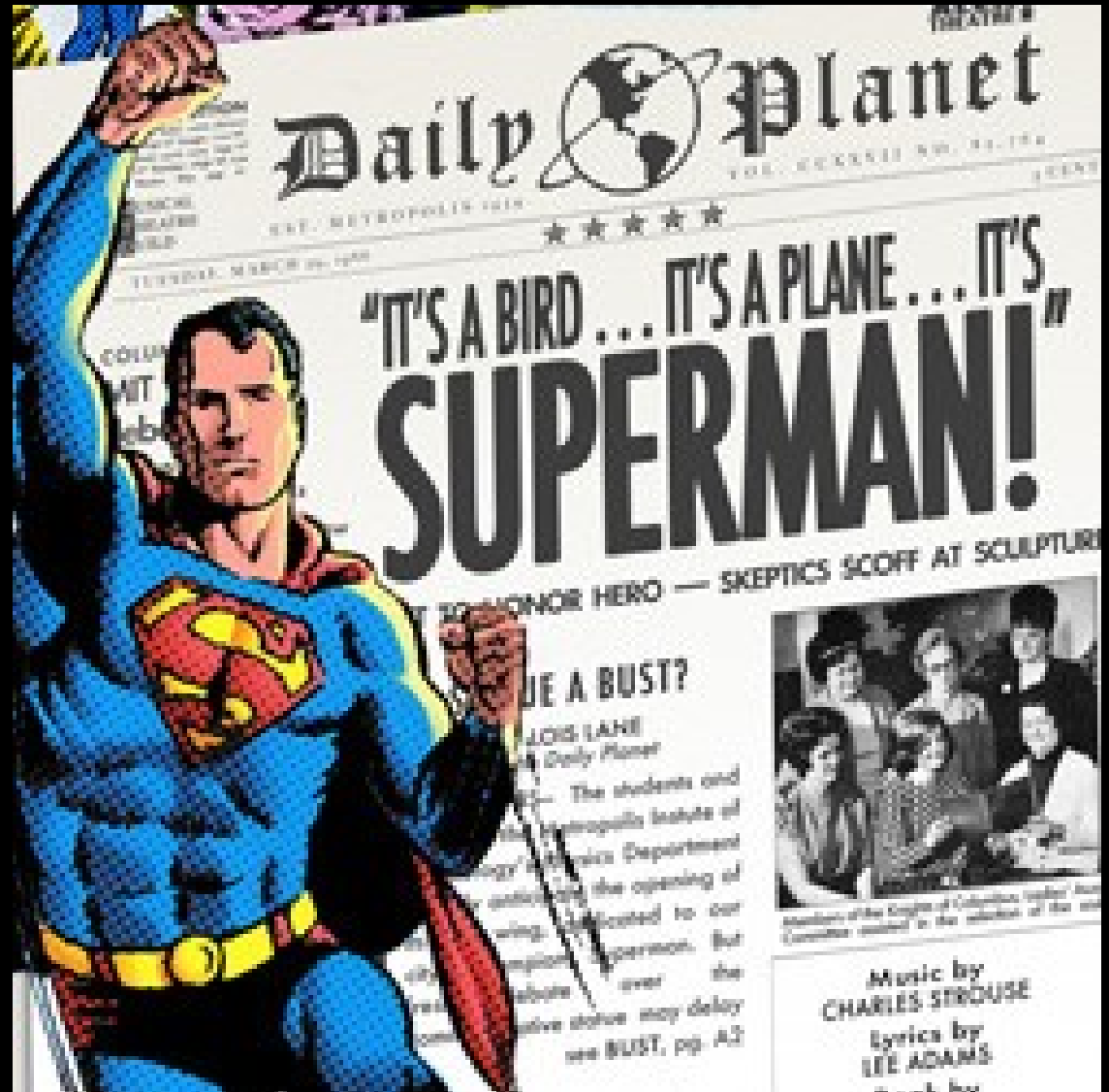
-It's scalar perturbations!

-It's topological defects!

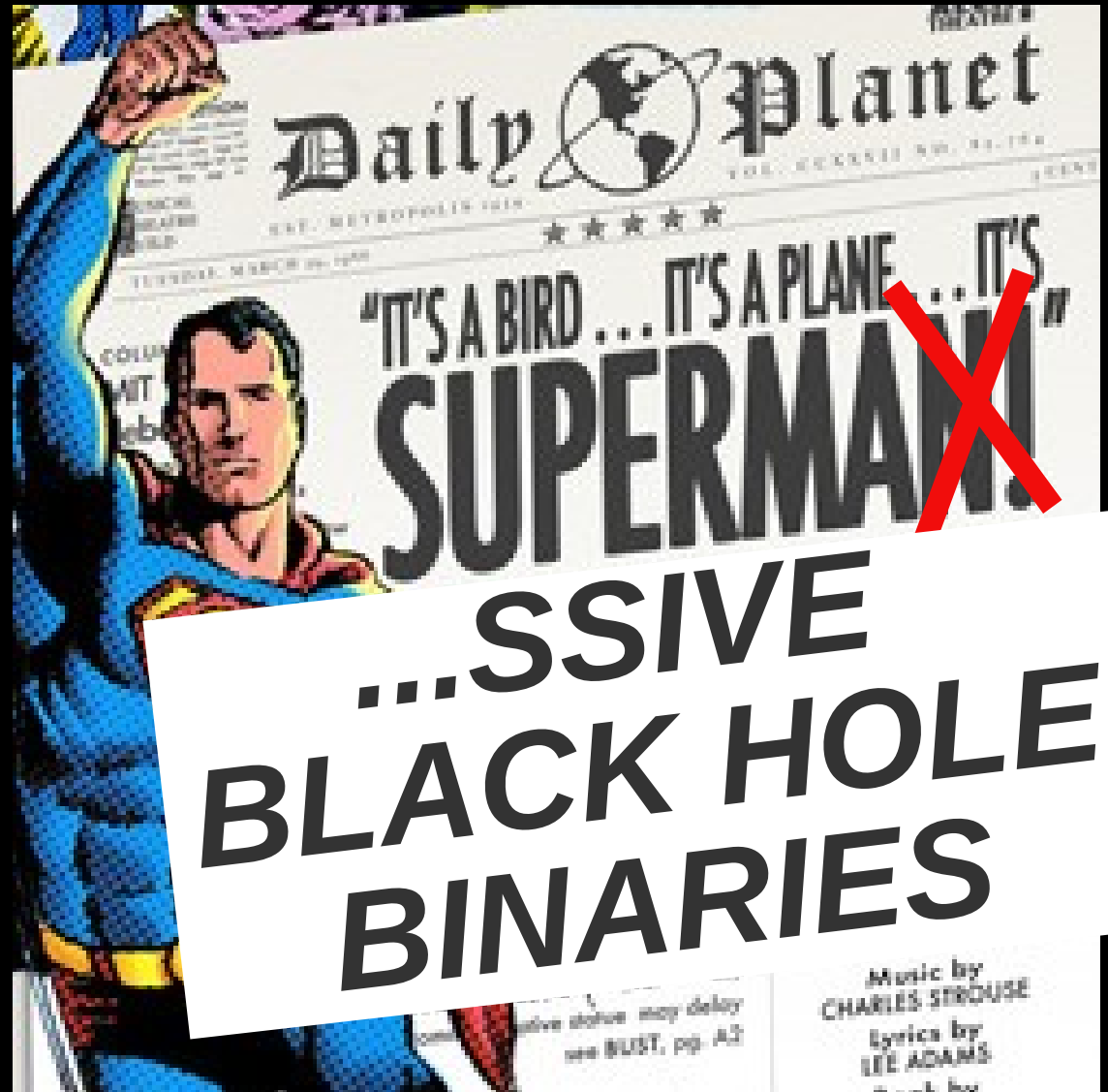
-It's domain walls!

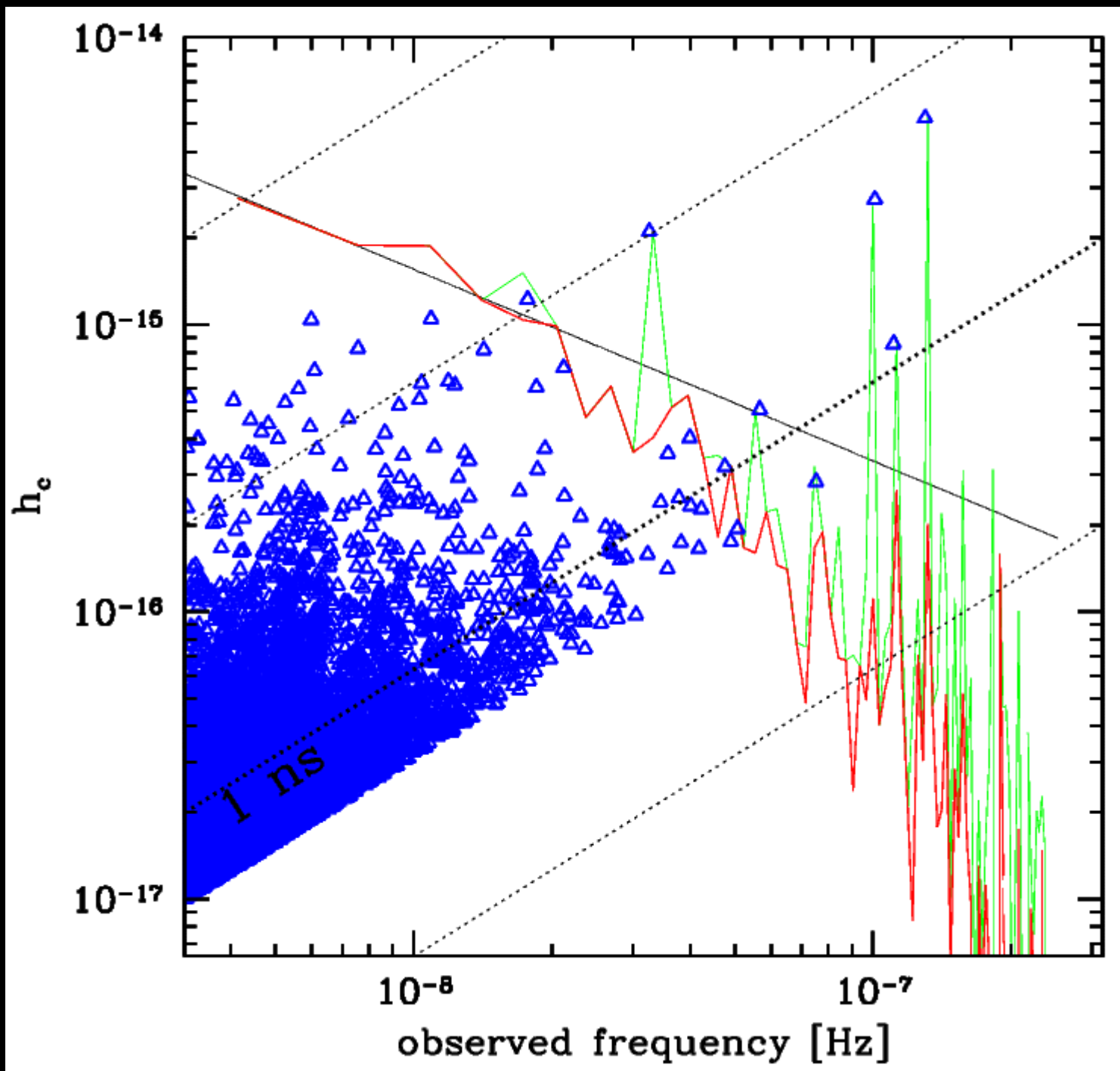
**-It's turbulence induced
perturbations!**

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- It's phase transitions!
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- It's domain walls!
- It's turbulence induced perturbations!





The overall GW signal

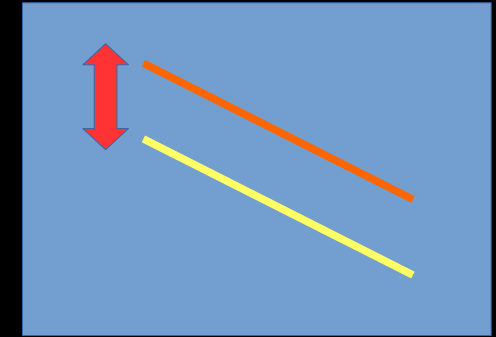
Population parameters

1-Galaxy merger rate \longleftrightarrow MBHB merger rate

affects the number of sources at each frequency $\rightarrow N_0$

2-MBH mass – merging galaxy relation

affects the mass of the sources $\rightarrow M_c$



$$h_c^2(f) = \int_0^\infty dz \int_0^\infty dM_1 \int_0^1 dq \frac{d^4 N}{dz dM_1 dq dt_r} \frac{dt_r}{d \ln f_{K,r}} \times$$

$$h^2(f_{K,r}) \sum_{n=1}^\infty \frac{g[n, e(f_{K,r})]}{(n/2)^2} \delta \left[f - \frac{n f_{K,r}}{1+z} \right].$$

$$h_c(f) \propto n_0^{1/2} f^{-\gamma} M_c^{5/6}$$

Local dynamics

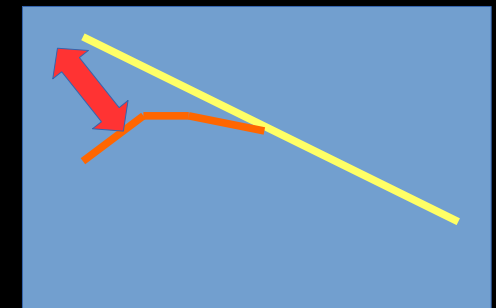
1-Accretion (when? how?)

affects the mass of the sources $\rightarrow M_c$

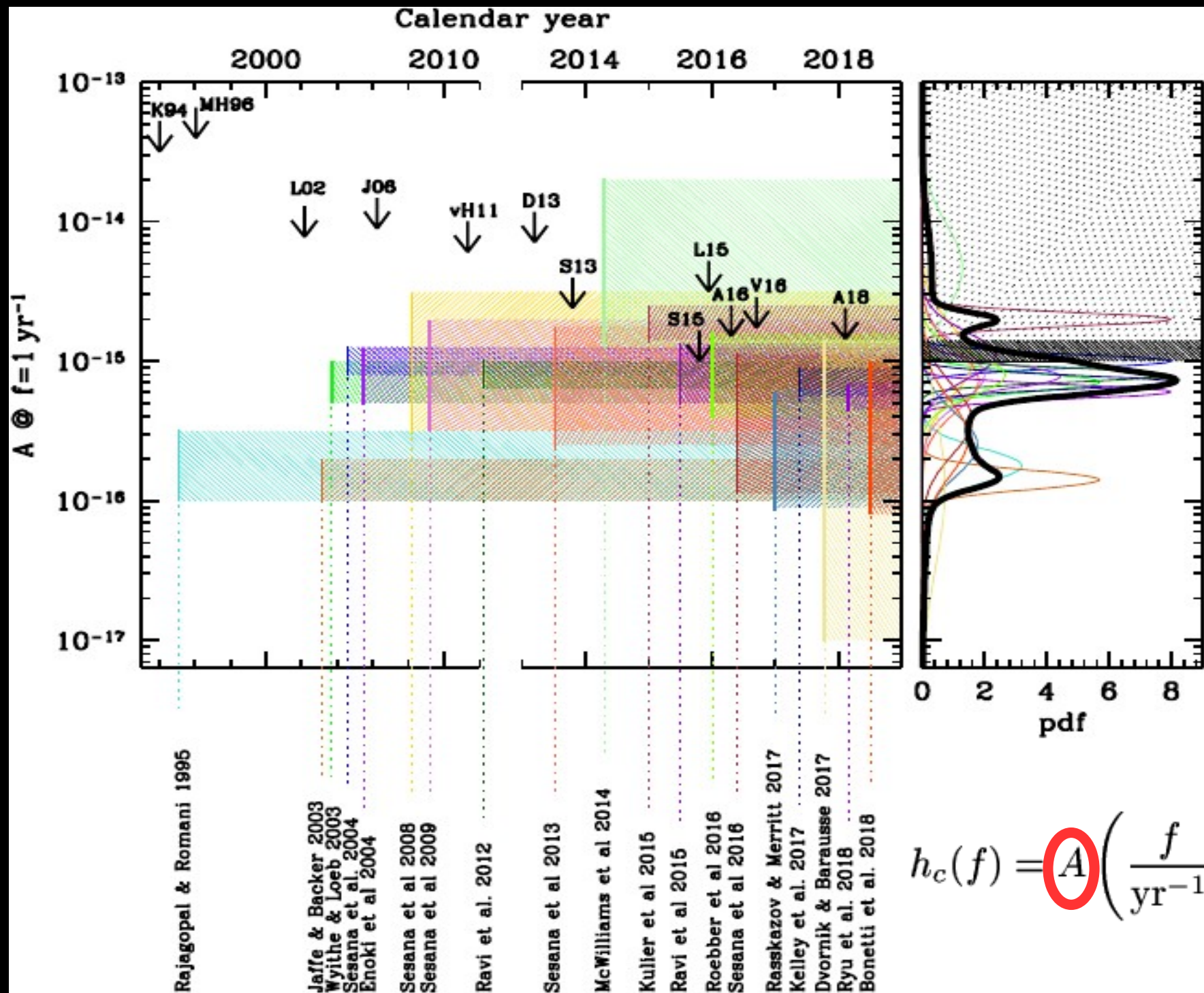
2-MBHB – environment coupling (gas & stars)

affects the chirping rate of the binaries $\rightarrow \gamma$

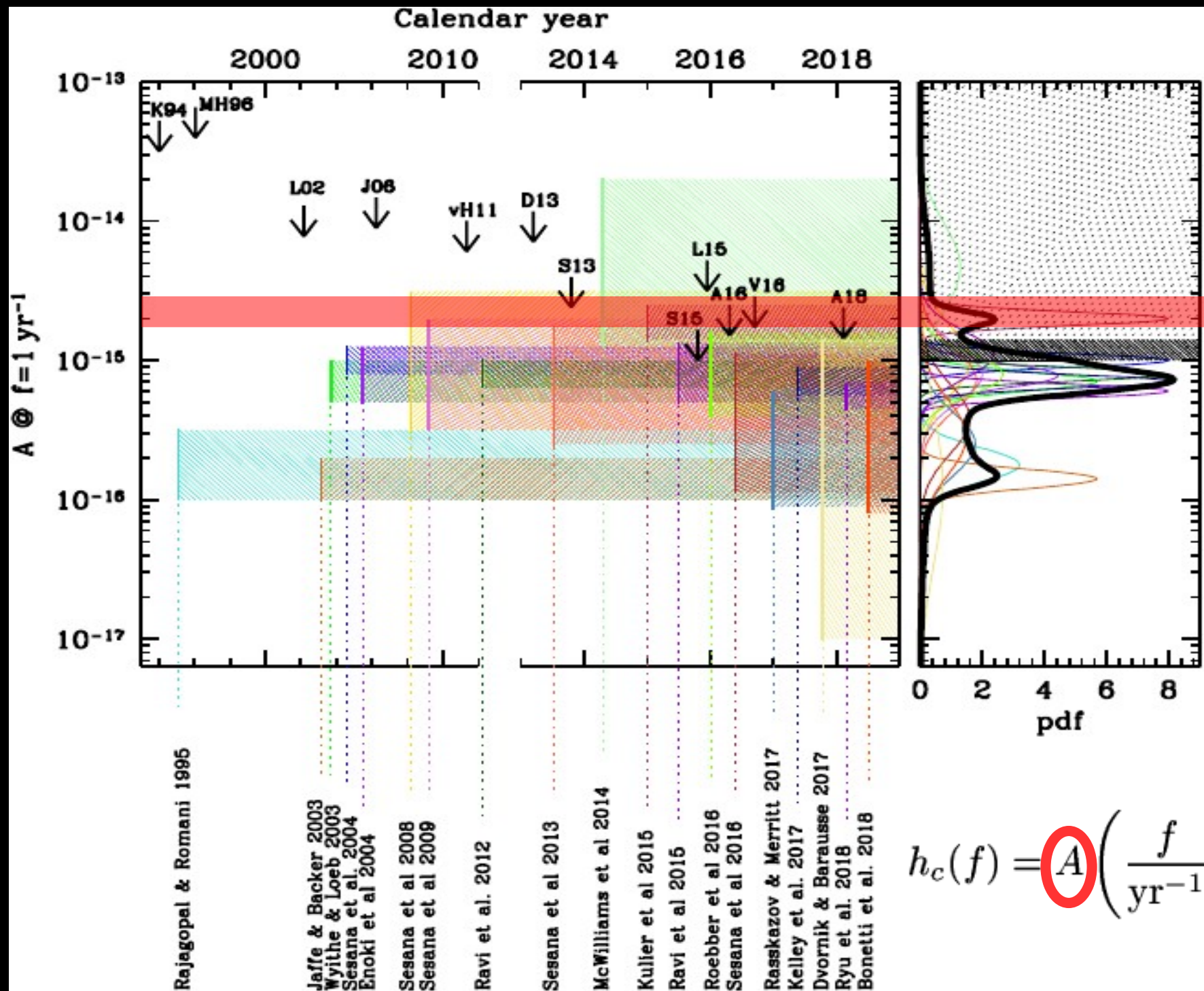
affects the eccentricity \rightarrow chirping rate $\rightarrow \gamma$ & single source detection



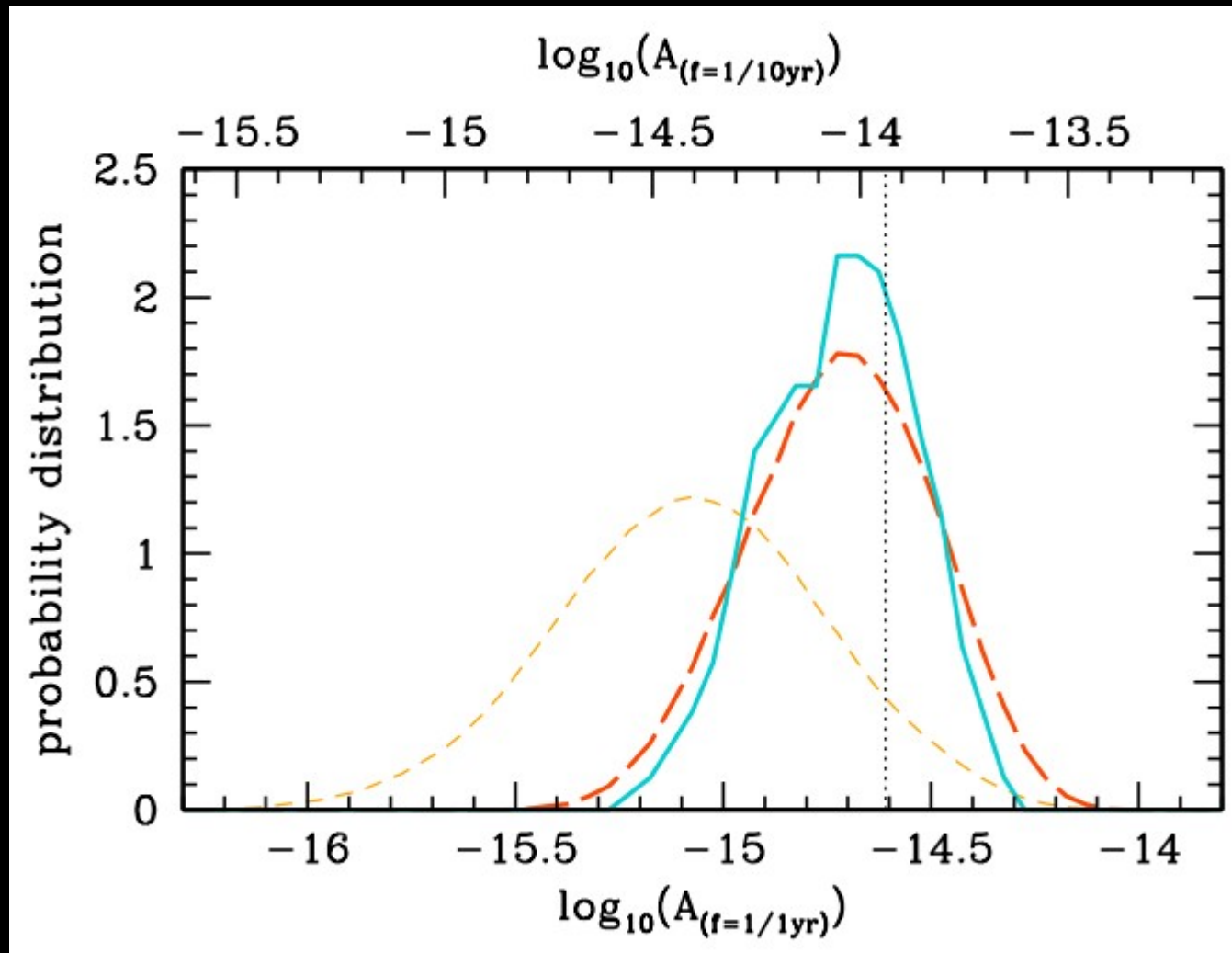
...Some predictions...



...Some predictions...



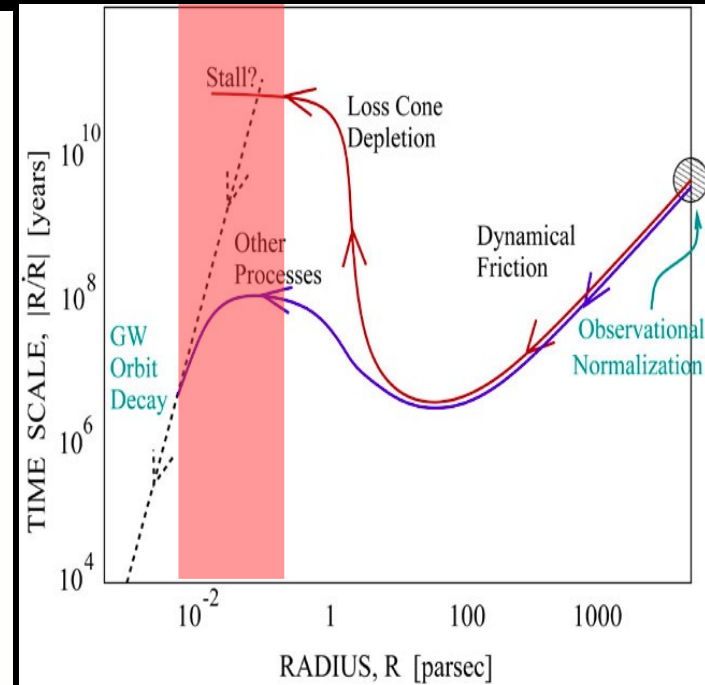
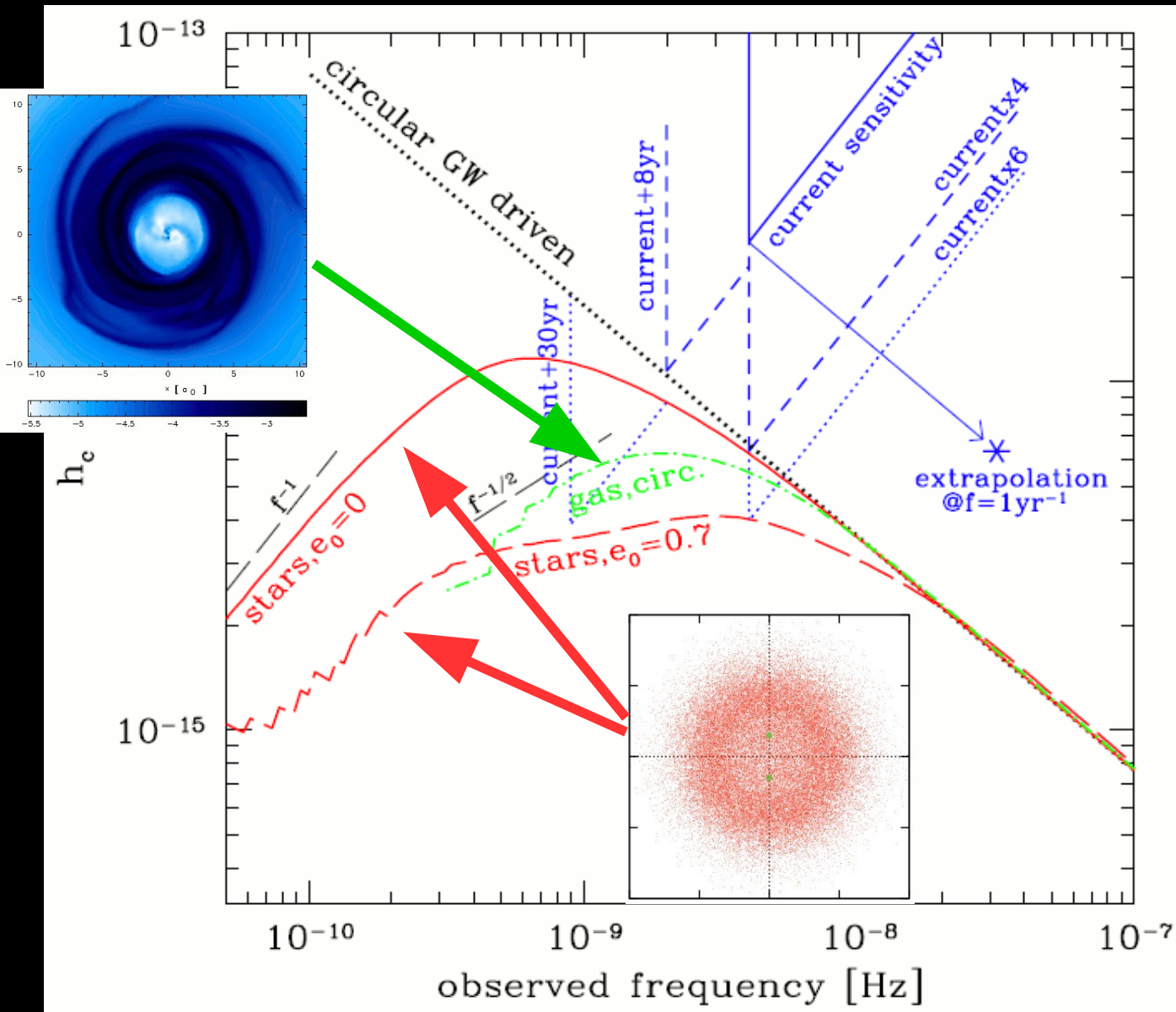
$$h_c(f) = A \left(\frac{f}{\text{yr}^{-1}} \right)^{-2/3}$$



This is **not a first principle calculation**, there's a lot of 'freedom'
Most notably:

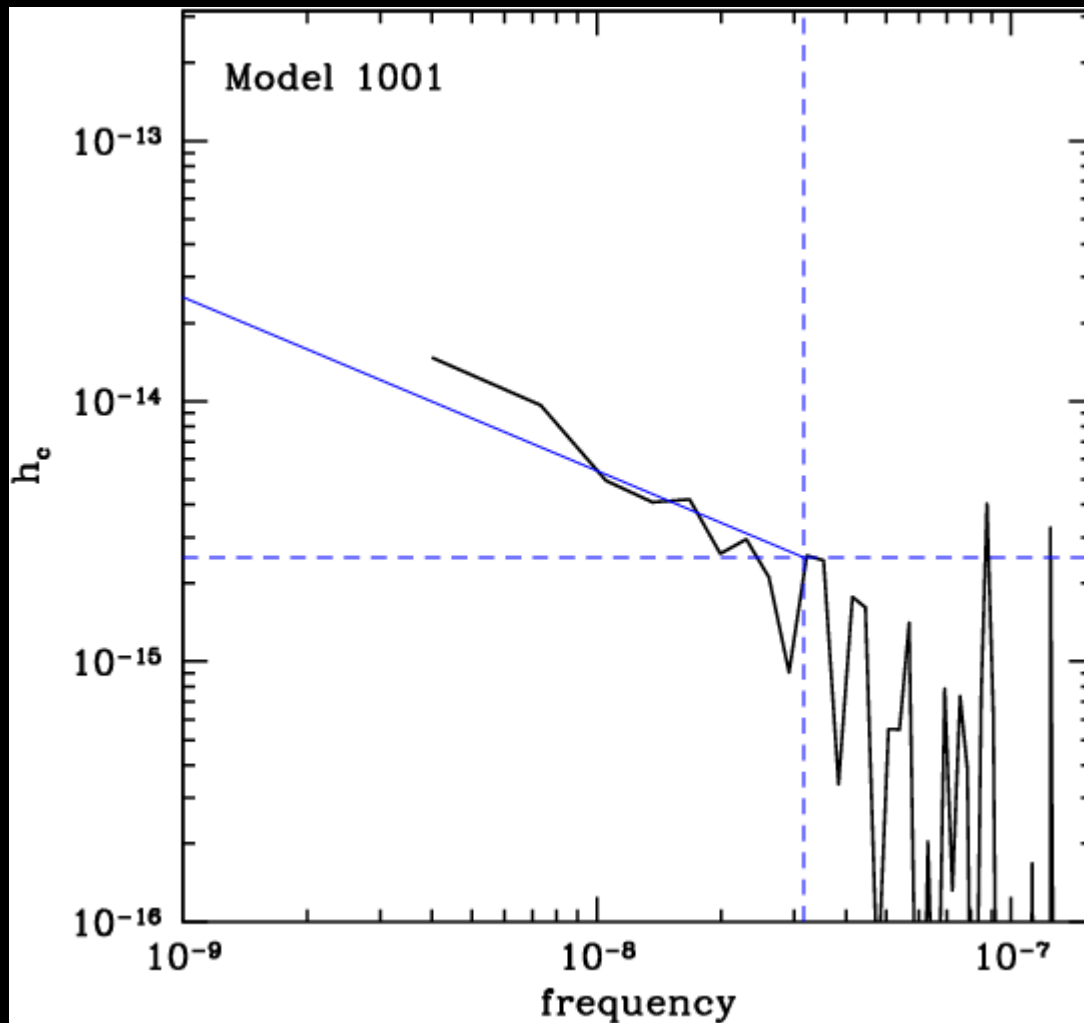
- MBH-galaxy relations (and their redshift evolution, e.g. Simon 2023)
- accretion during mergers (Before? After? Onto the primary? Secondary?)

Uncertainty in the GW background shape



(Kocsis & AS 2011, AS 2013, Ravi et al. 2014, McWilliams et al. 2014)

Qualitative comparison with empirical models



Qualitative comparison with Rosado+15 models

- Merger rate determined observationally (S13) via galaxy mass function, pair fraction, merger time etc etc...

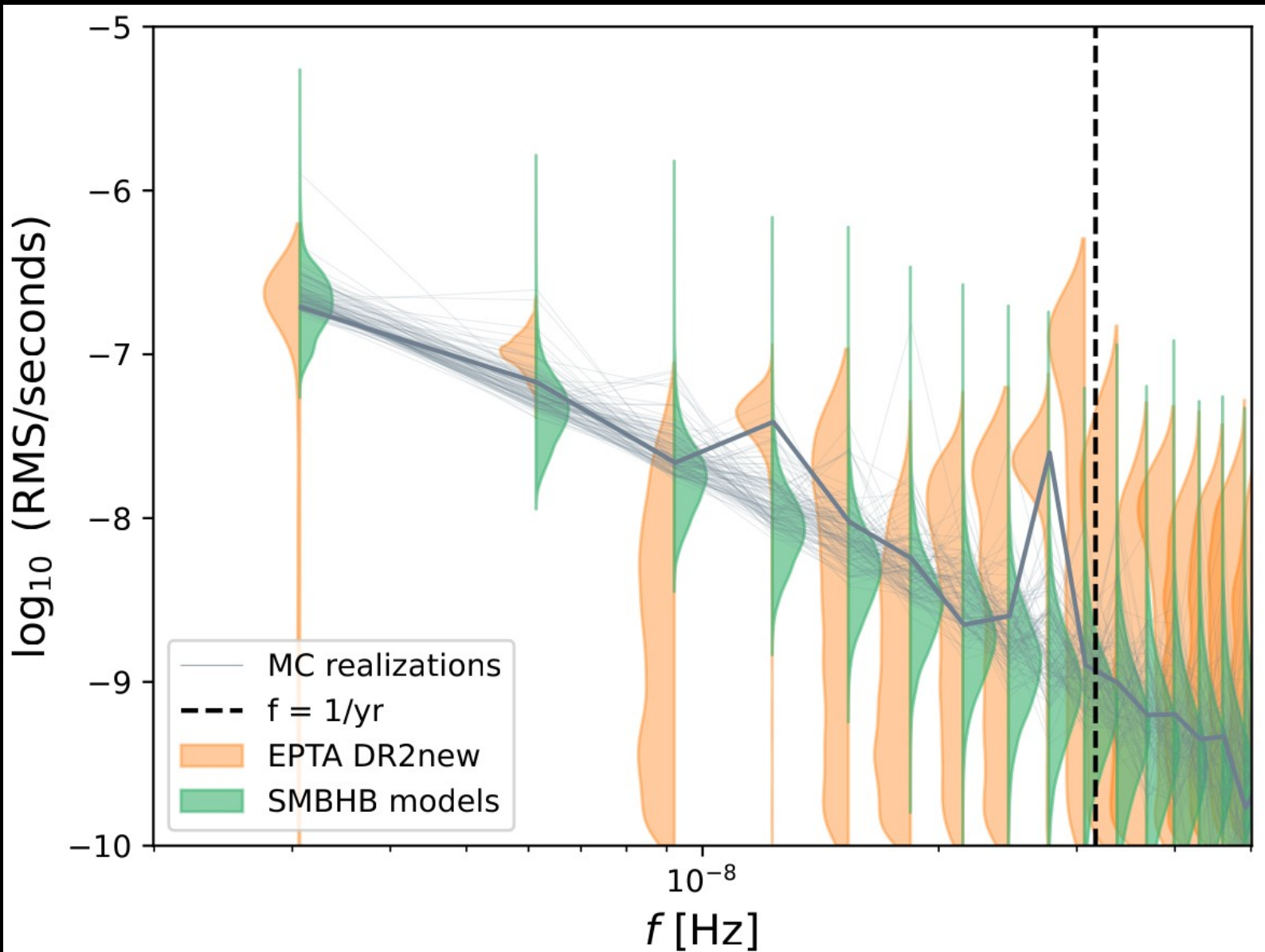
- constrained by observations

- adding hardening via stars and eccentricity (S10)

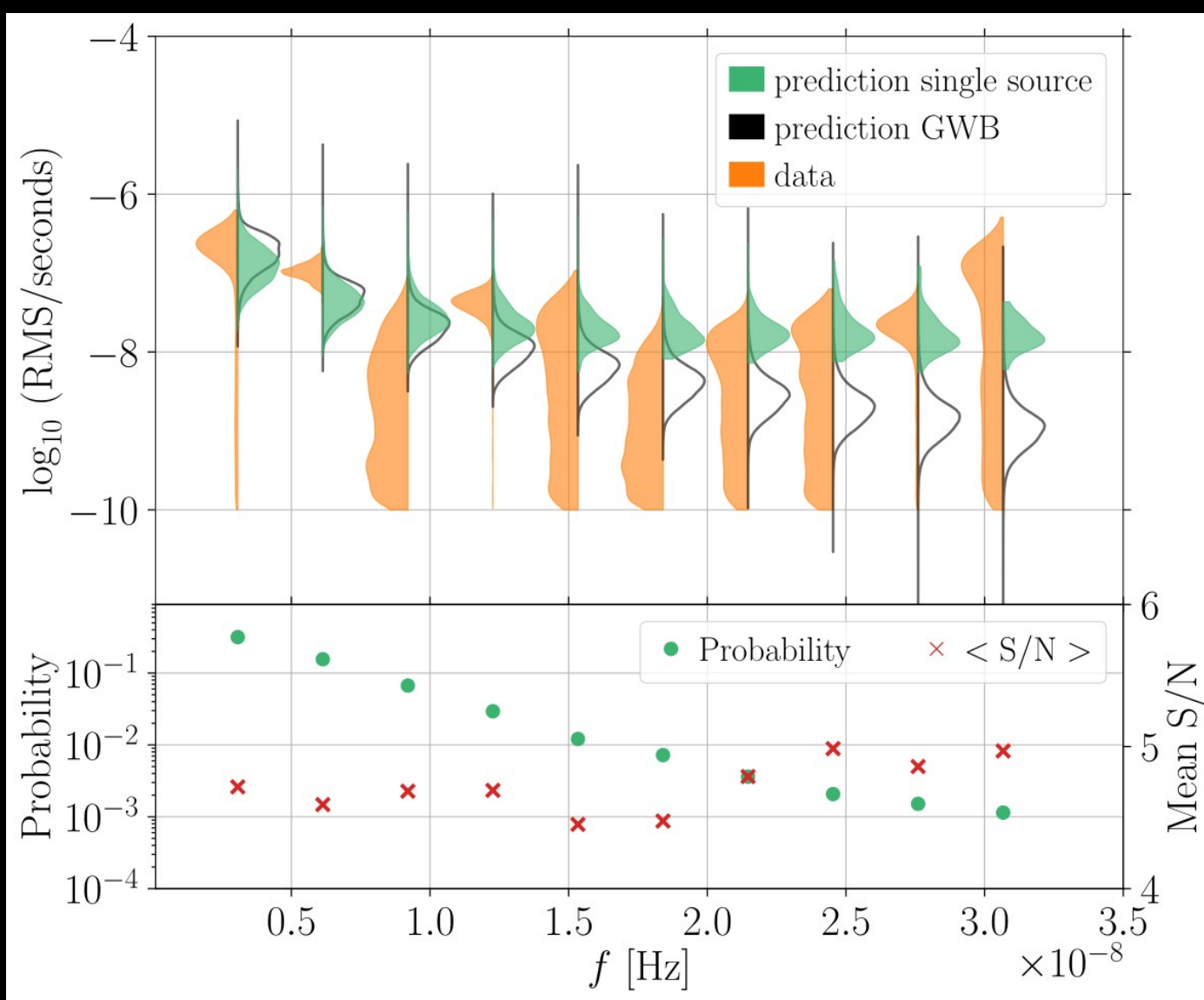
324k MC realizations

- captures signal variance

- capture resolvable sources

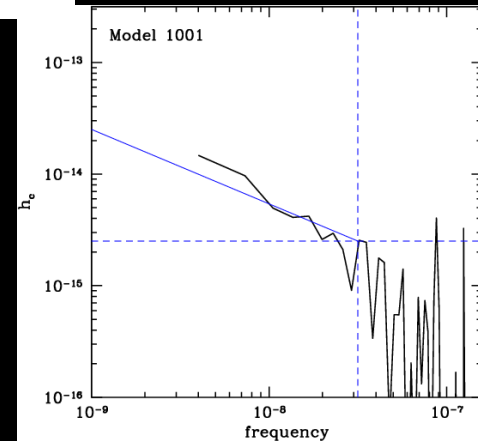


Free spectrum in good agreement with measurements (9 bins)
Excess power measured at the 9th bin (flat $\gamma \sim 3$)

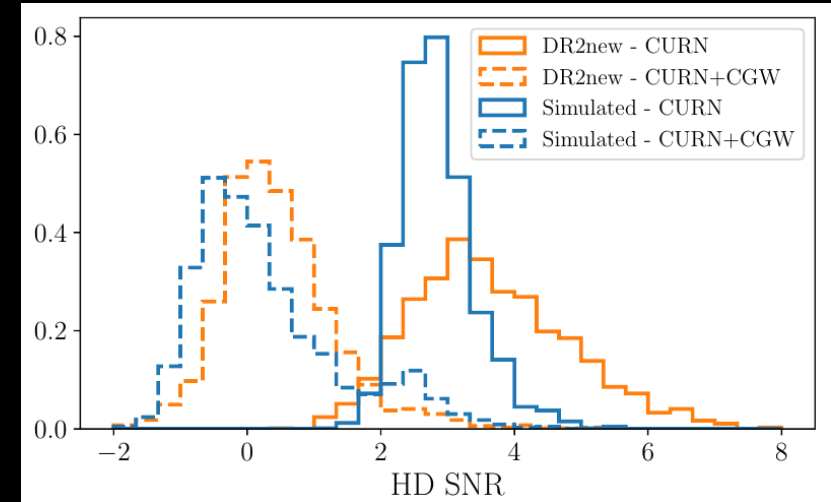
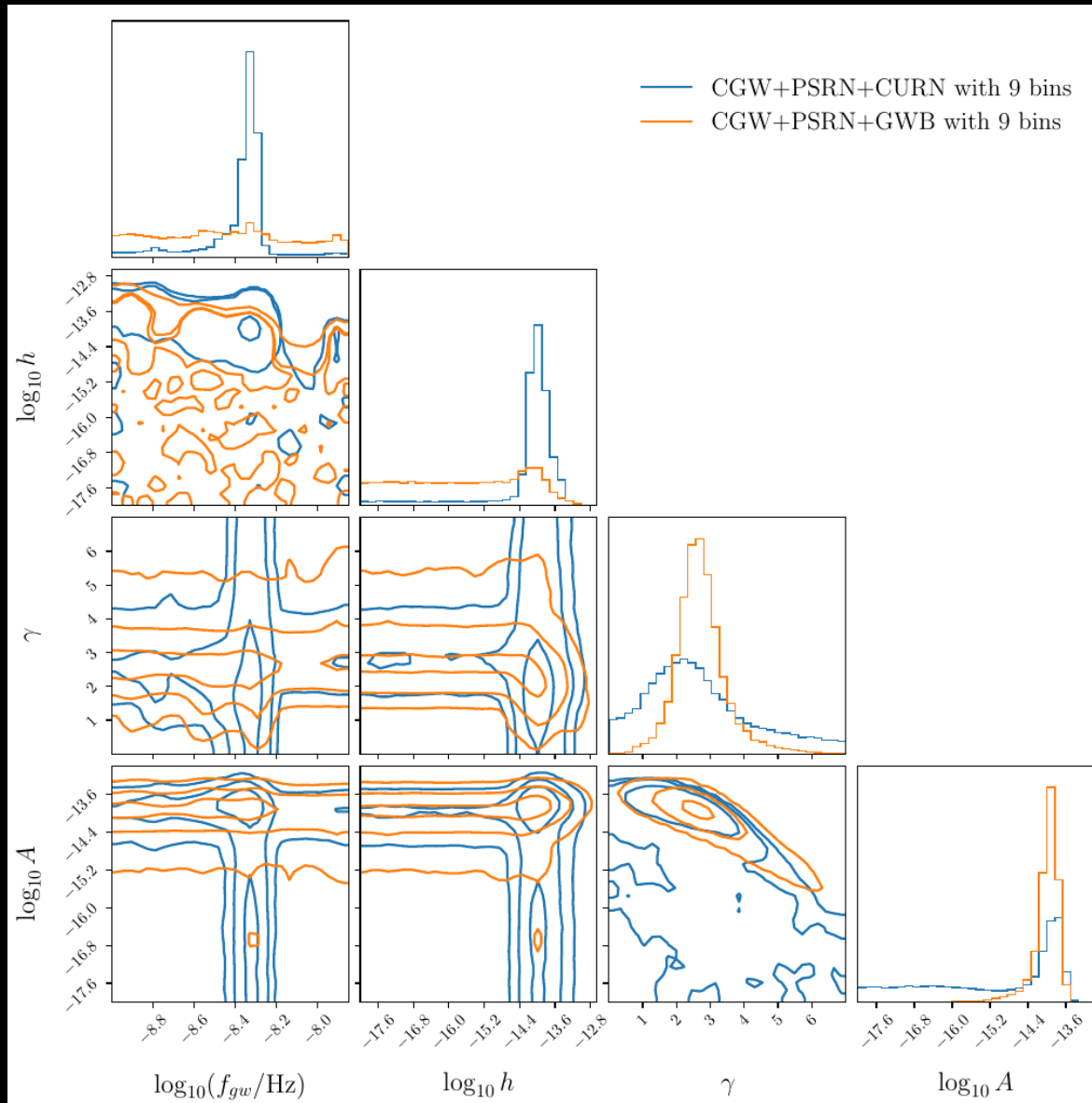


Models allow to compute CGW detection statistics (circular, SNR>3)

~50% probability to have at least a CGW (mostly at the lowest frequency) (higher than Becsy+2022, but lower SNR threshold)



Assessing the type of signal is NOT trivial



Data can be fit by an individual continuous GW (CGW)

Strongly preferred over common noise....

...but absorbed by the GWB

Simulations show that it can be difficult to discriminate between CGW and GWB at this stage

SMBHB inference from the data

Agnostic models

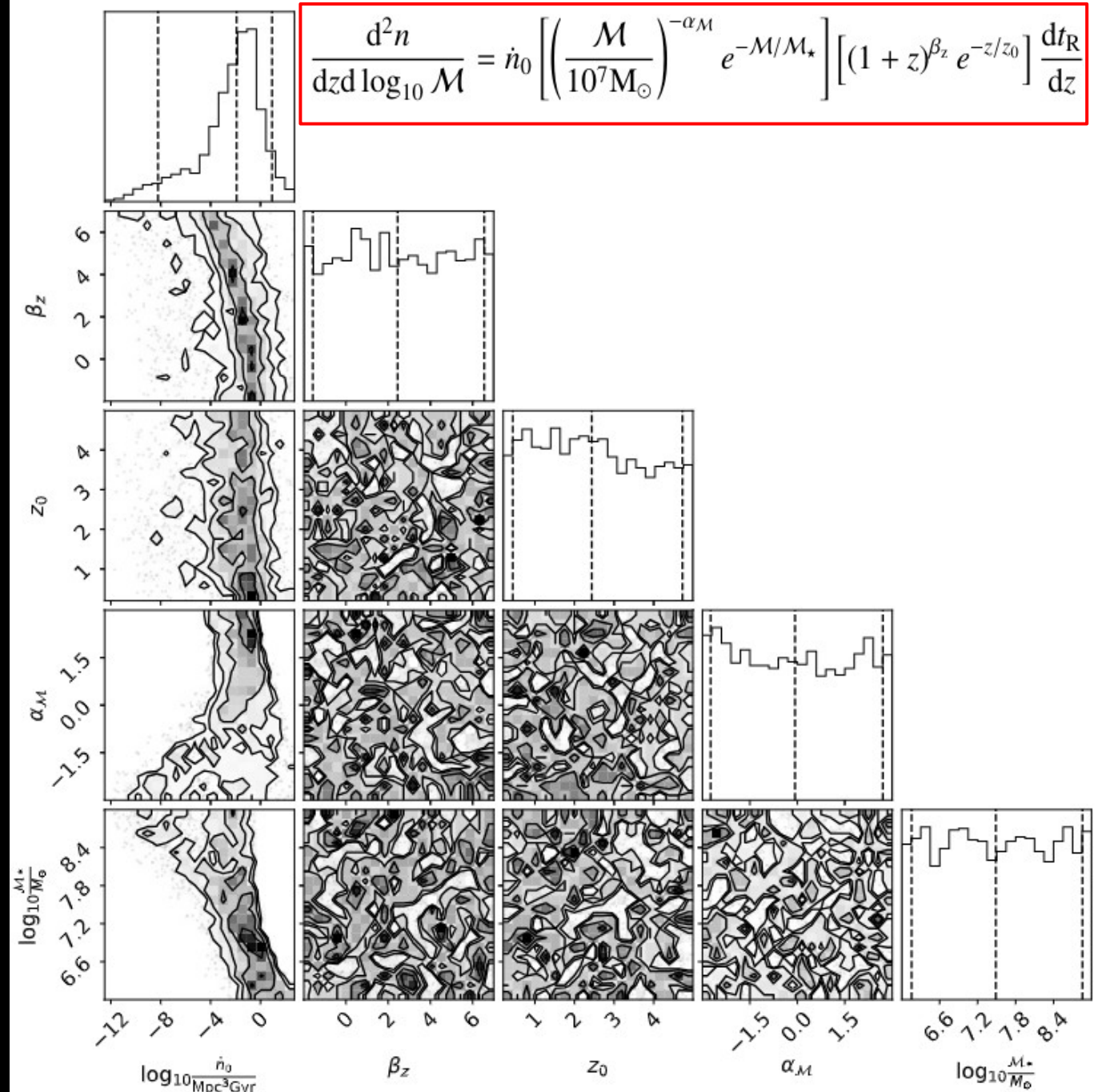
(Middleton+16)

-general mass function
(Schechter + z dependence)

-no other constraints

-circular binary

Only constrain: SMBHB
merger density



$$\frac{d^3 n_G}{dz' dM dq} = \frac{\Phi(M, z)}{M \ln 10} \frac{\mathcal{F}(M, z, q)}{\tau(M, z, q)} \frac{dt}{dz}$$

Astro constrained models
(Chen+19)

-generalization of

Rosado+15

-informed by observations:

-Galaxy mass function

-Galaxy pair fraction

$$f_{\text{pair}} = f_0 \left(\frac{M}{10^{11} M_\odot} \right)^{\alpha_f} (1+z)^{\beta_f}$$

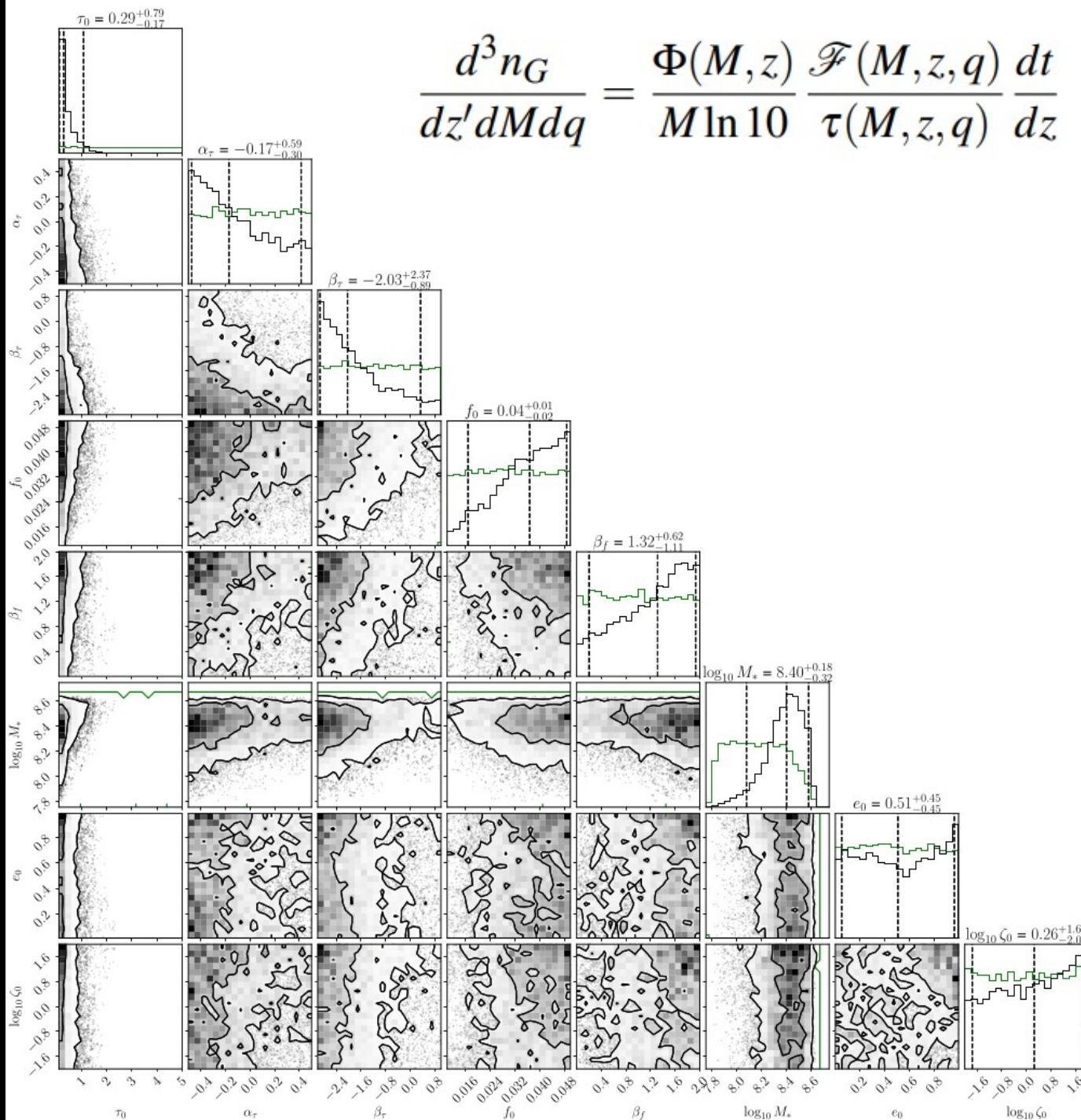
-SMBHB merger timescale

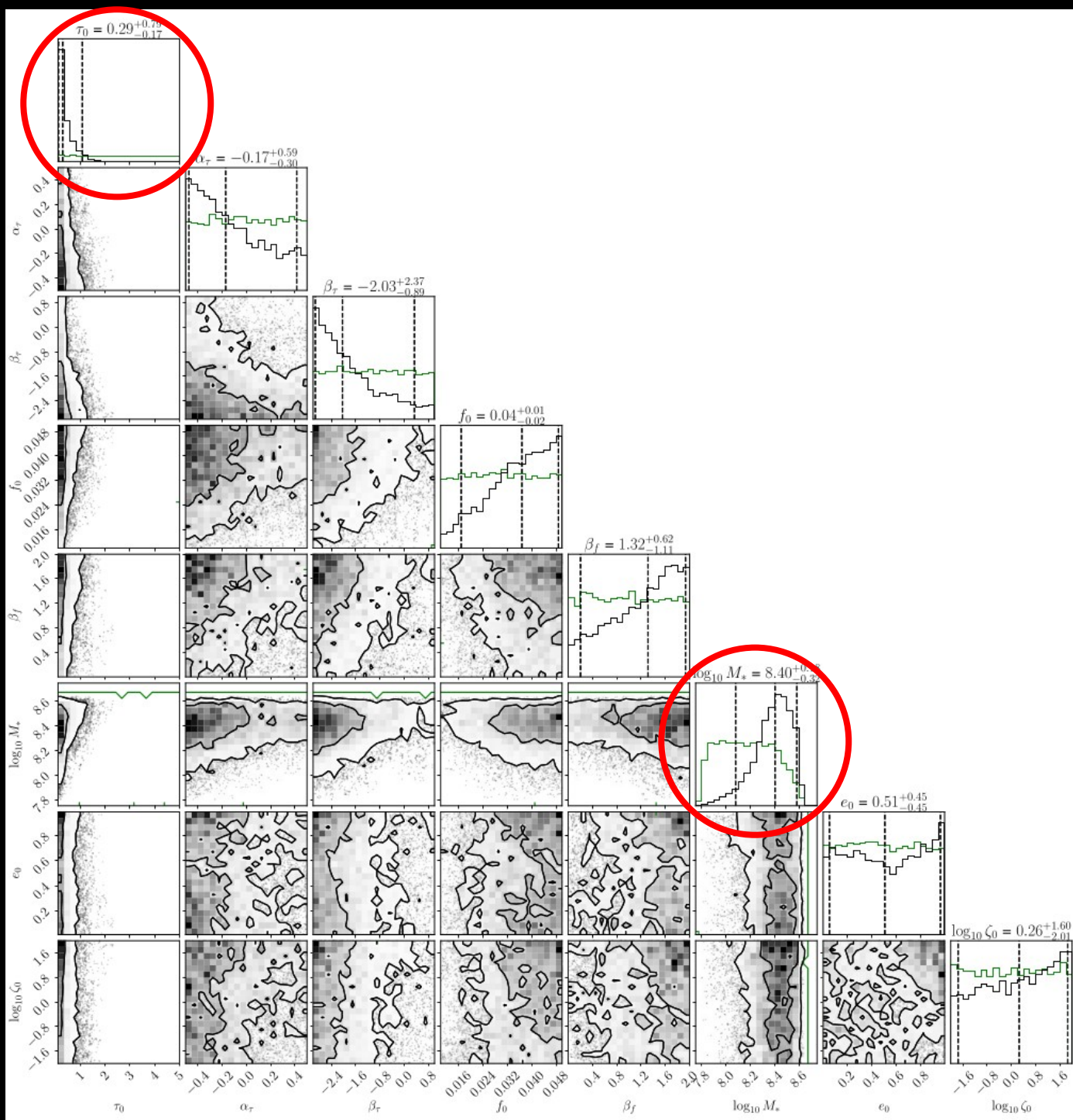
$$\tau = \tau_0 \left(\frac{M}{10^{11} M_\odot} \right)^{\alpha_\tau} (1+z)^{\beta_\tau} q^{\gamma_\tau}$$

-SMBH-galaxy relation

$$m = \mathcal{N} \left\{ M_* \left(\frac{M_b}{10^{11} M_\odot} \right)^{\alpha_*}, \epsilon \right\}$$

-eccentricity and
environment





Astro constrained models
(Chen+19)

-generalization of

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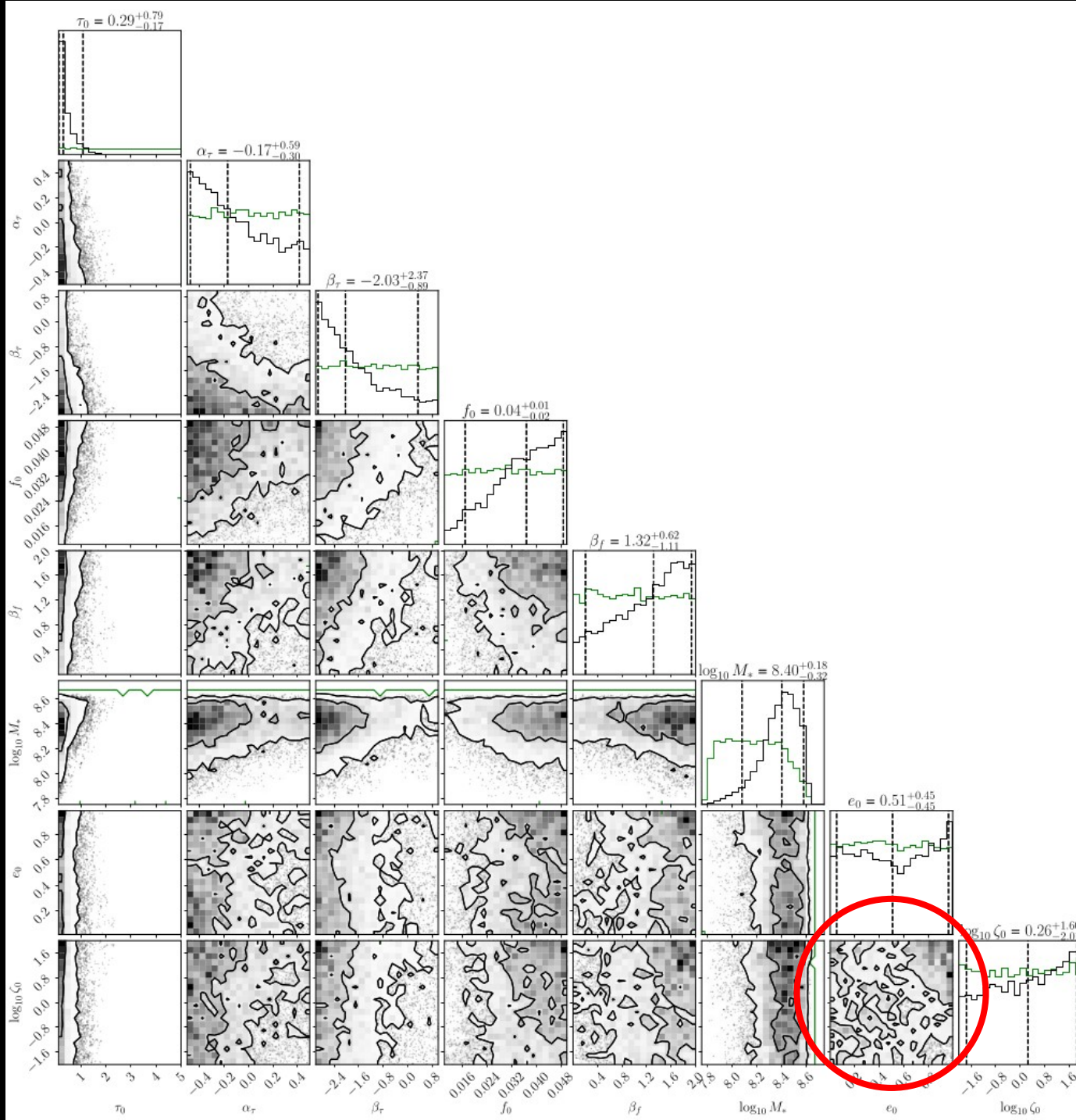
-eccentricity and
environment

Best constrains:

-SMBHB time to merger

-SMBH – M_* relation

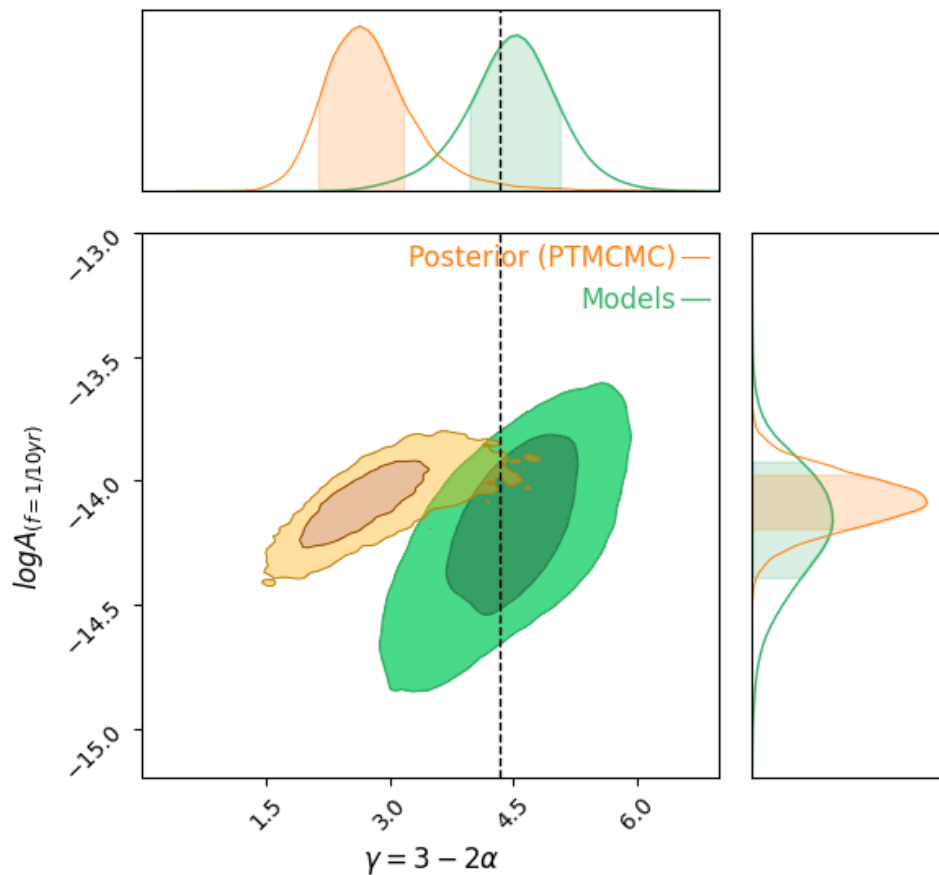
SMBHB are massive and merge frequently



SMBHB are massive and merge frequently

- Astro constrained models (Chen+19)**
- generalization of Rosado+15
 - informed by observations:
 - Galaxy mass function
 - Galaxy pair fraction
 - SMBHB merger timescale
 - SMBH-galaxy relation
 - eccentricity and environment
- Best constrains:**
- SMBHB time to merger
 - SMBH – M_* relation
 - Slight preference for eccentric/dense environments

Powerlaw fitted to 9 bins



A- gamma plots broadly consistent

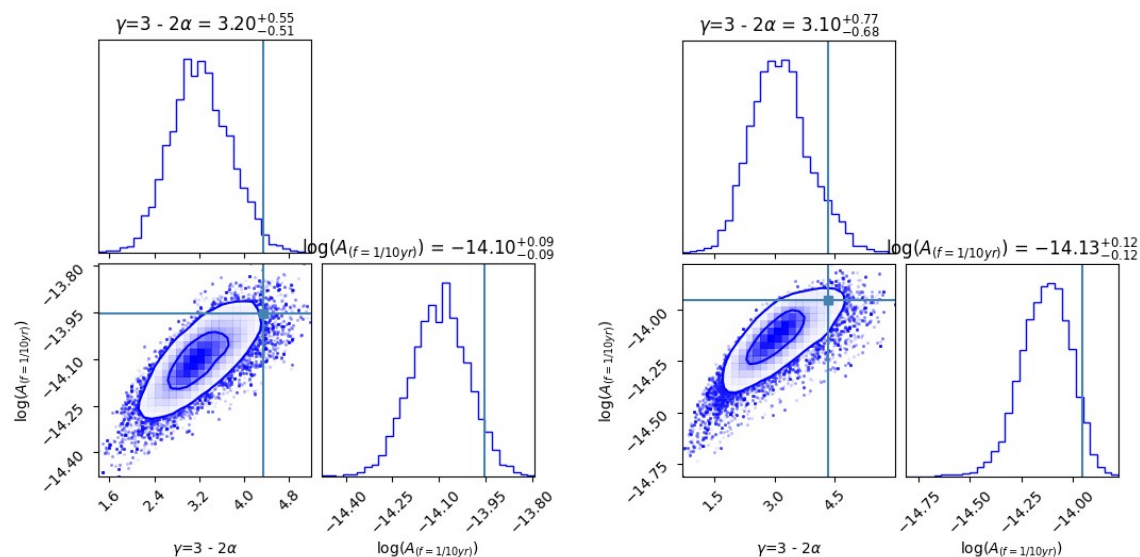
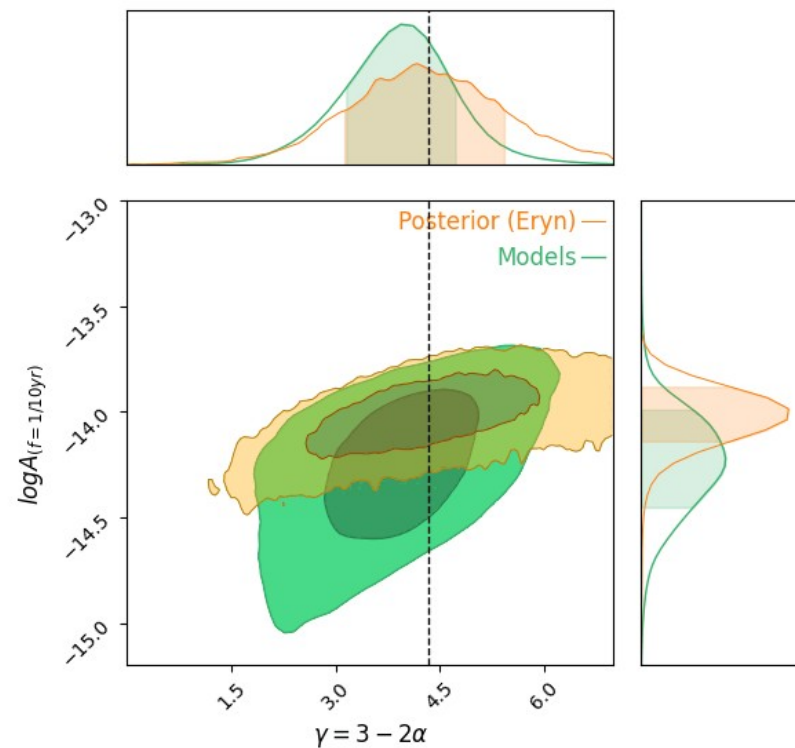
A normalized @1/10yr

Warning:

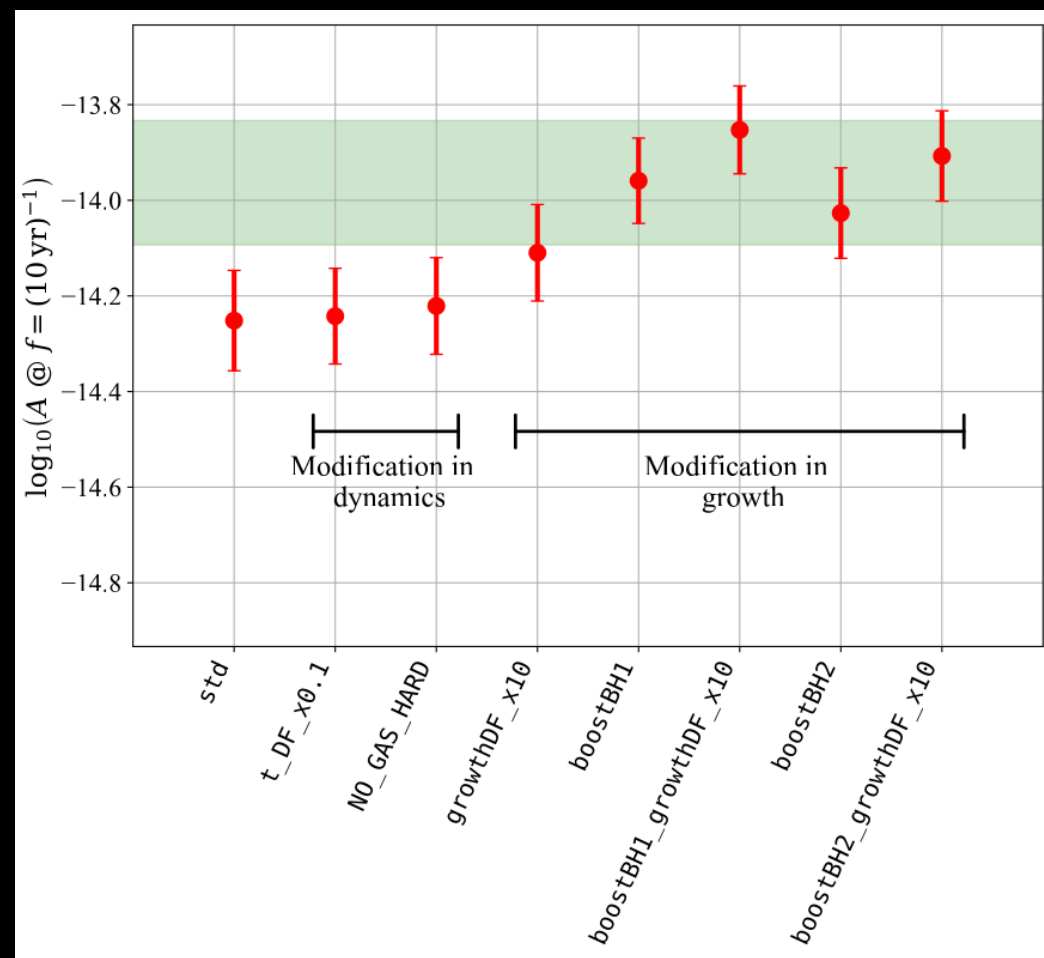
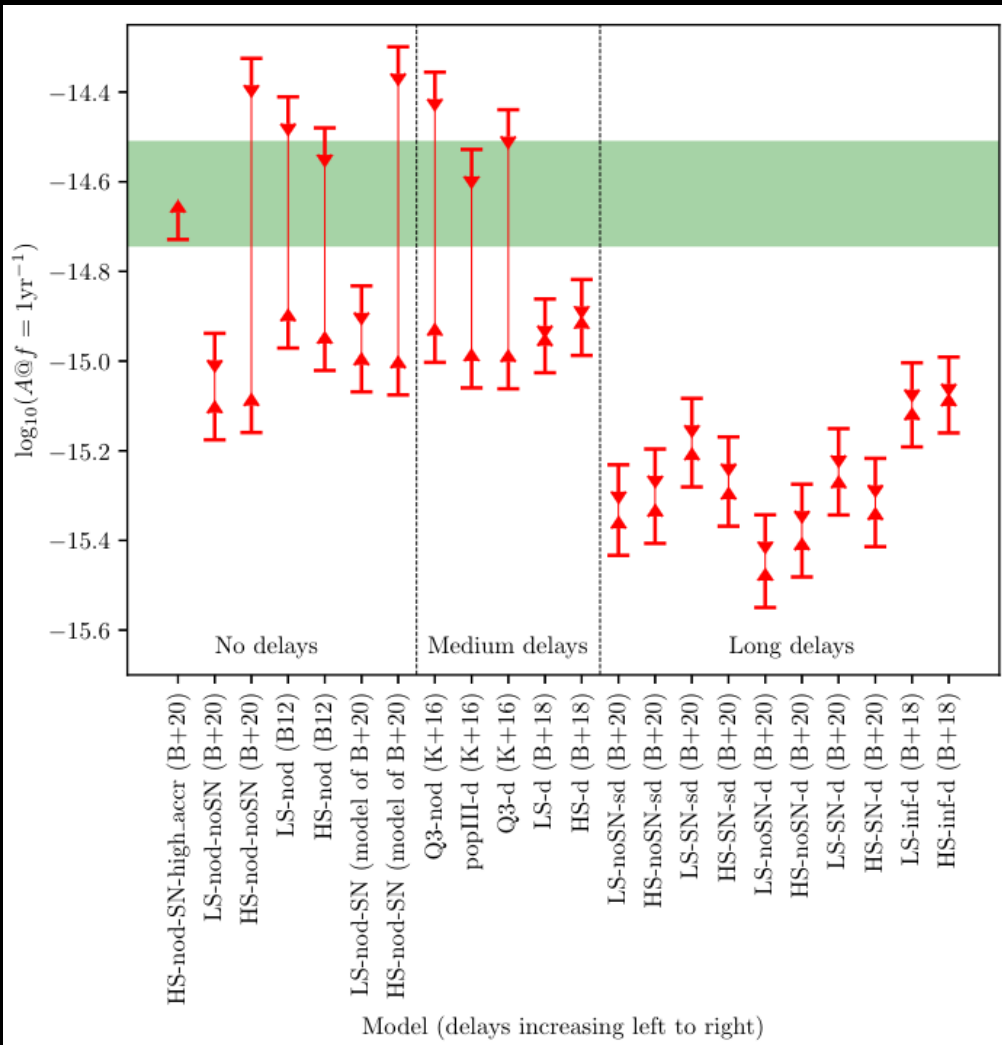
-fits and measurements depend on numbers of bin

-measured flat value could be due to low SNR

Powerlaw fitted to 3 bins



Comparison with semianalytic models



Barausse12

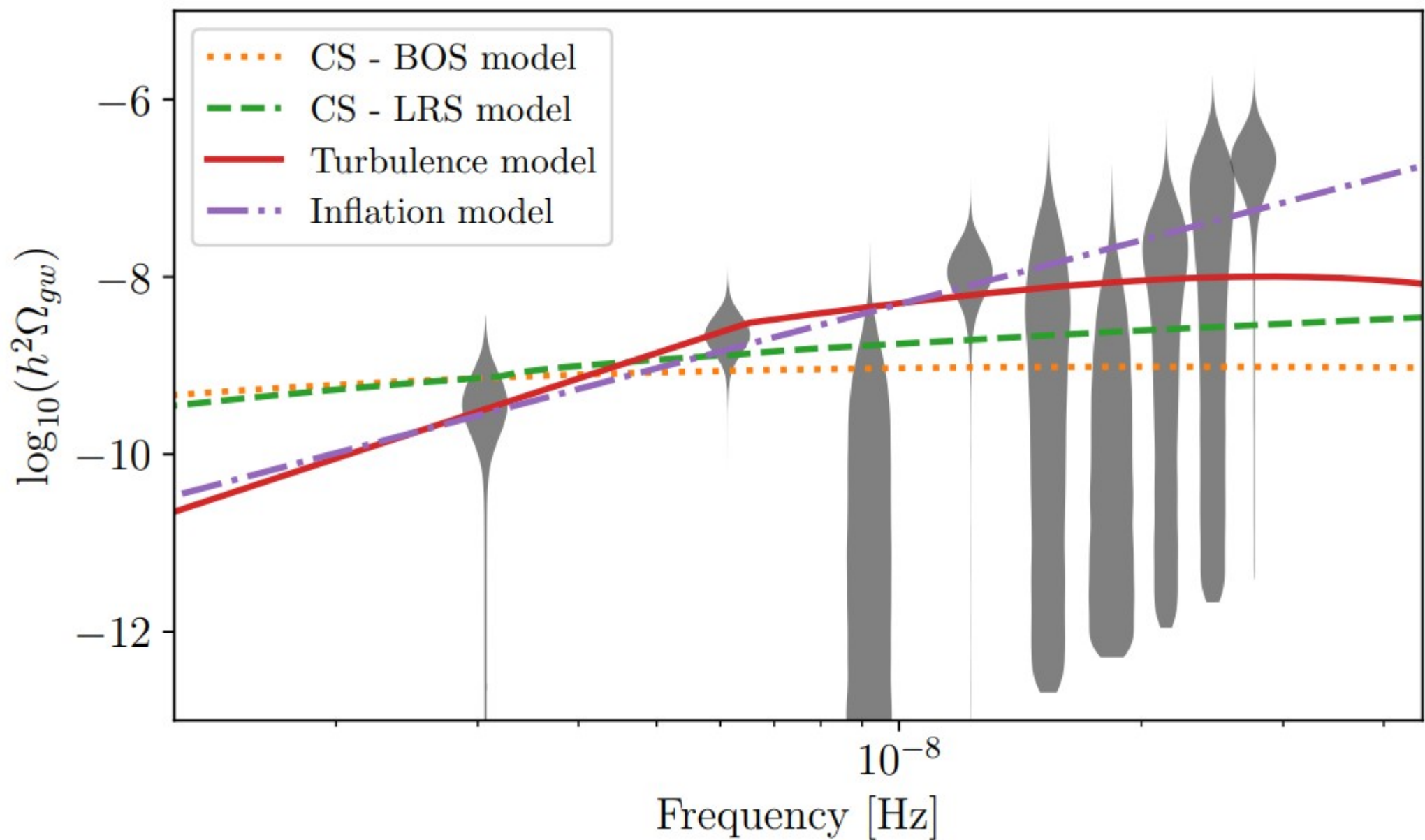
- hard to reproduce the observed amplitude
- higher resolution can help
- short delays favoured

L-Galaxies

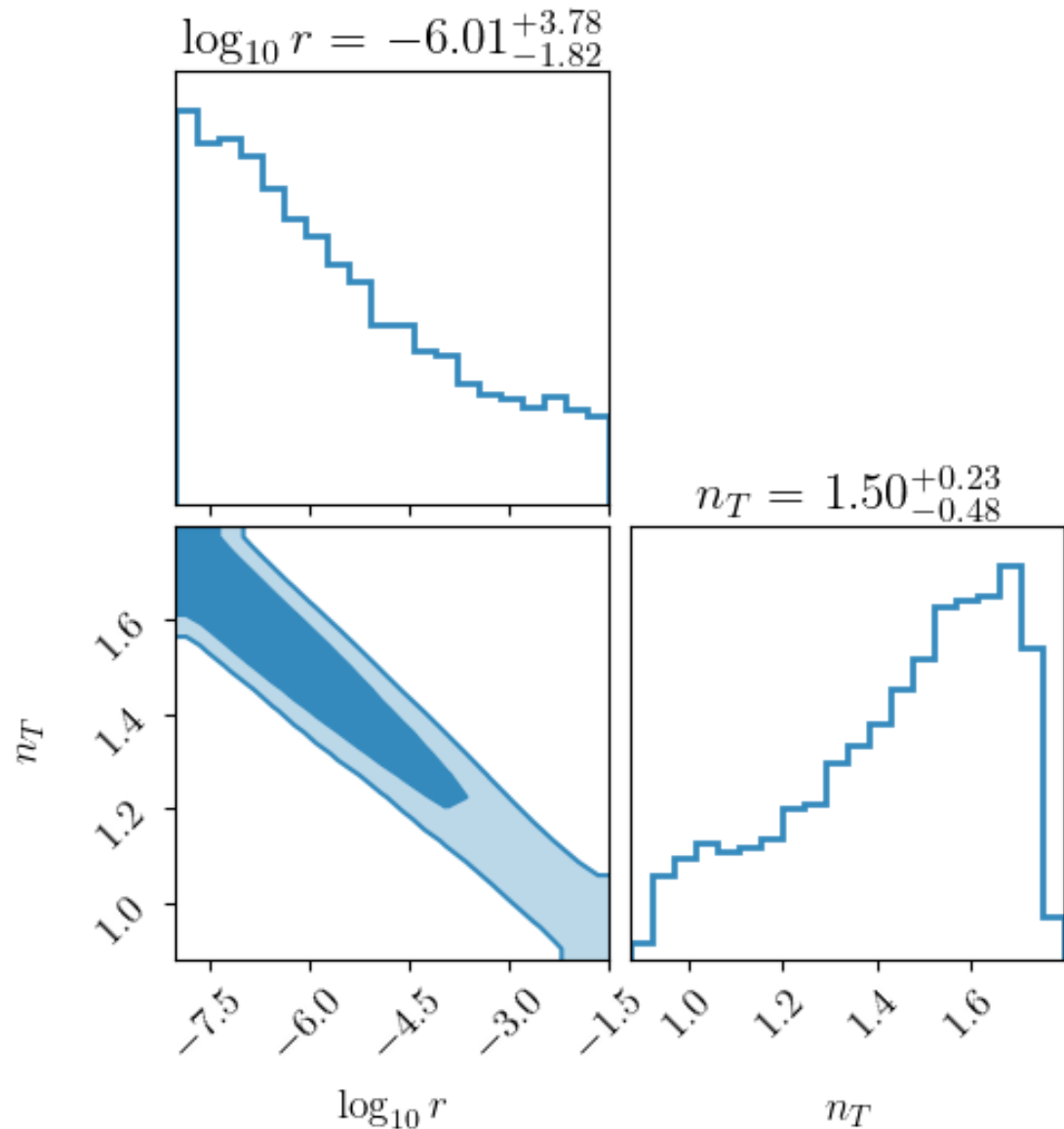
- hard to reproduce the observed amplitude
- needs boosting of the SMBH growth
- might run into problems with quasar L func

Non trivial constraints to SAMs

Early Universe



Early Universe: I. Inflation



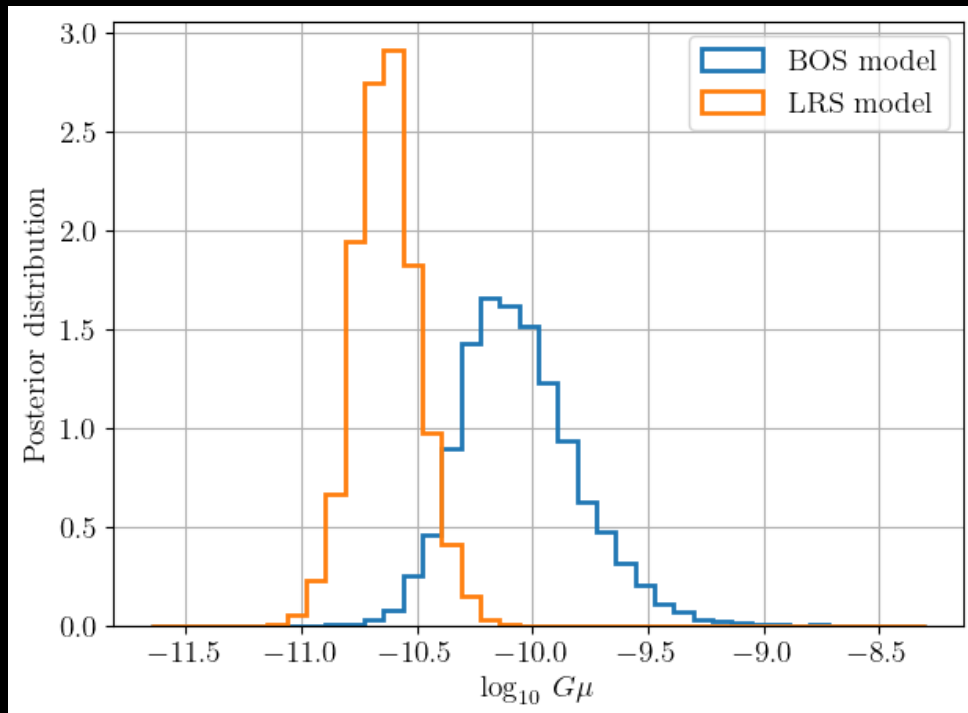
Ingredient of the standard cosmological model

Occurs shortly after the Big Bang

Strong correlation n_T - r

Inflation interpretation implies $n_T > 1$ and $\log_{10} r < -4$

Early Universe: II. Cosmic strings

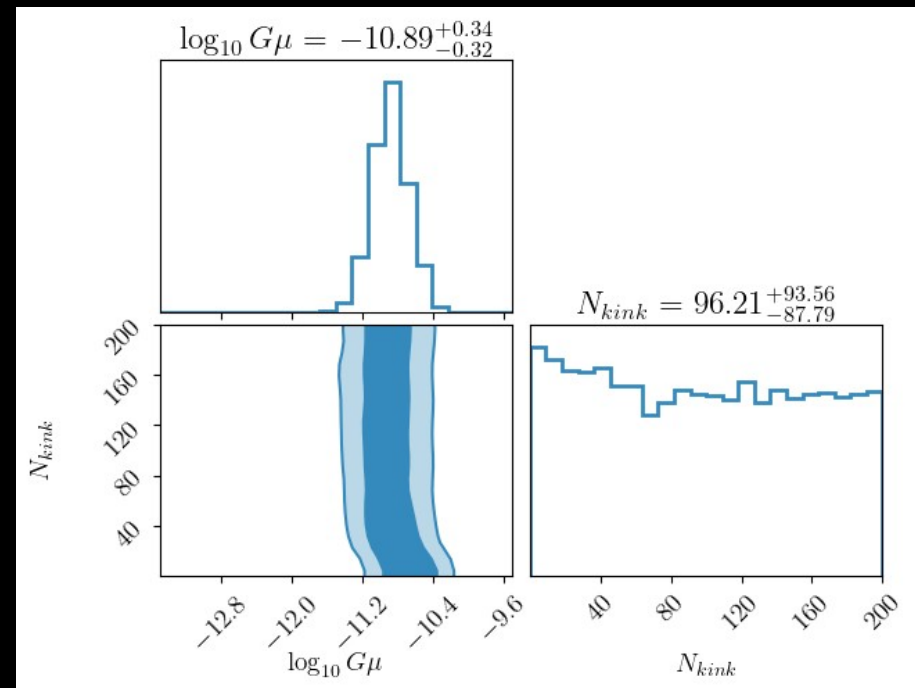
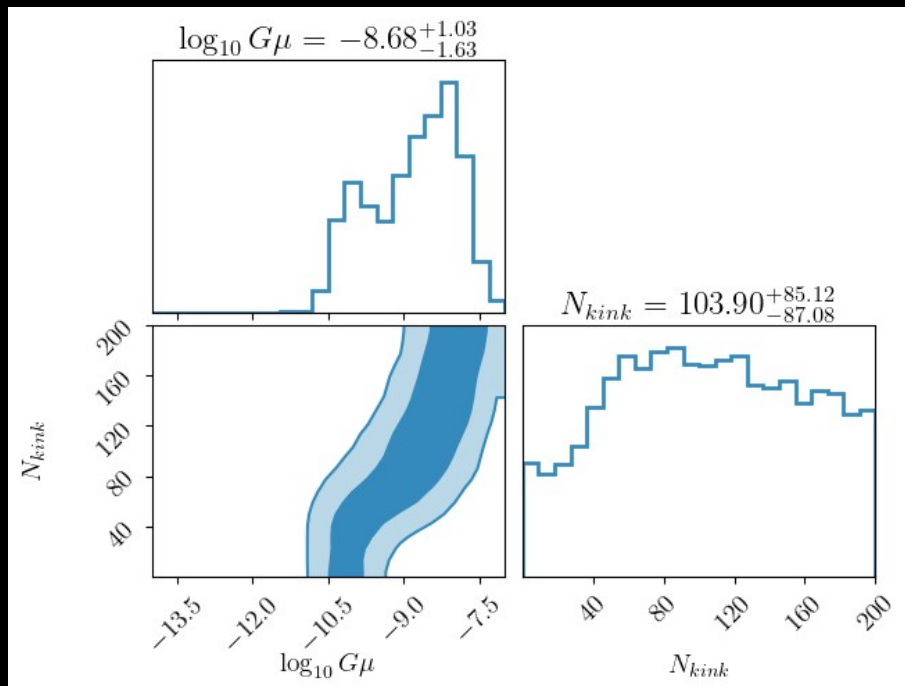


Produce GWs through decay of loops and kinks.

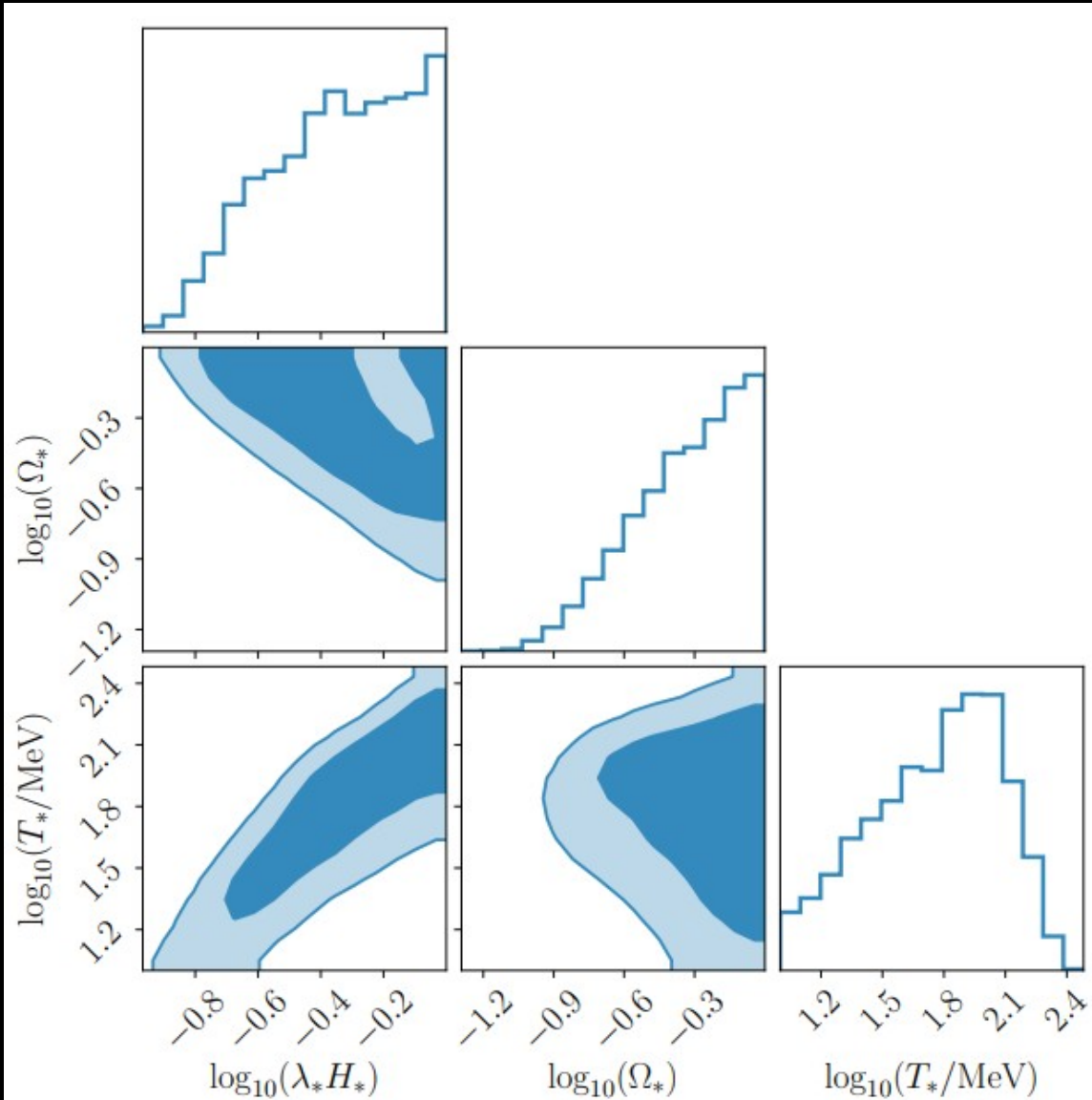
GWB at low frequency can constrain the string tension parameter.

DR2 measurement consistent with $-11 < \log_{10} G\mu < -9.5$

Kinks unconstrained



Early Universe: III. 1st order QCD phase transitions



- T_* : temperature at which the GW spectrum is originated

-\mathbf{\lambda_*H_*} : characteristic length scale of the magnetic energy spectrum

-\mathbf{\Omega_M} : magnetic energy density

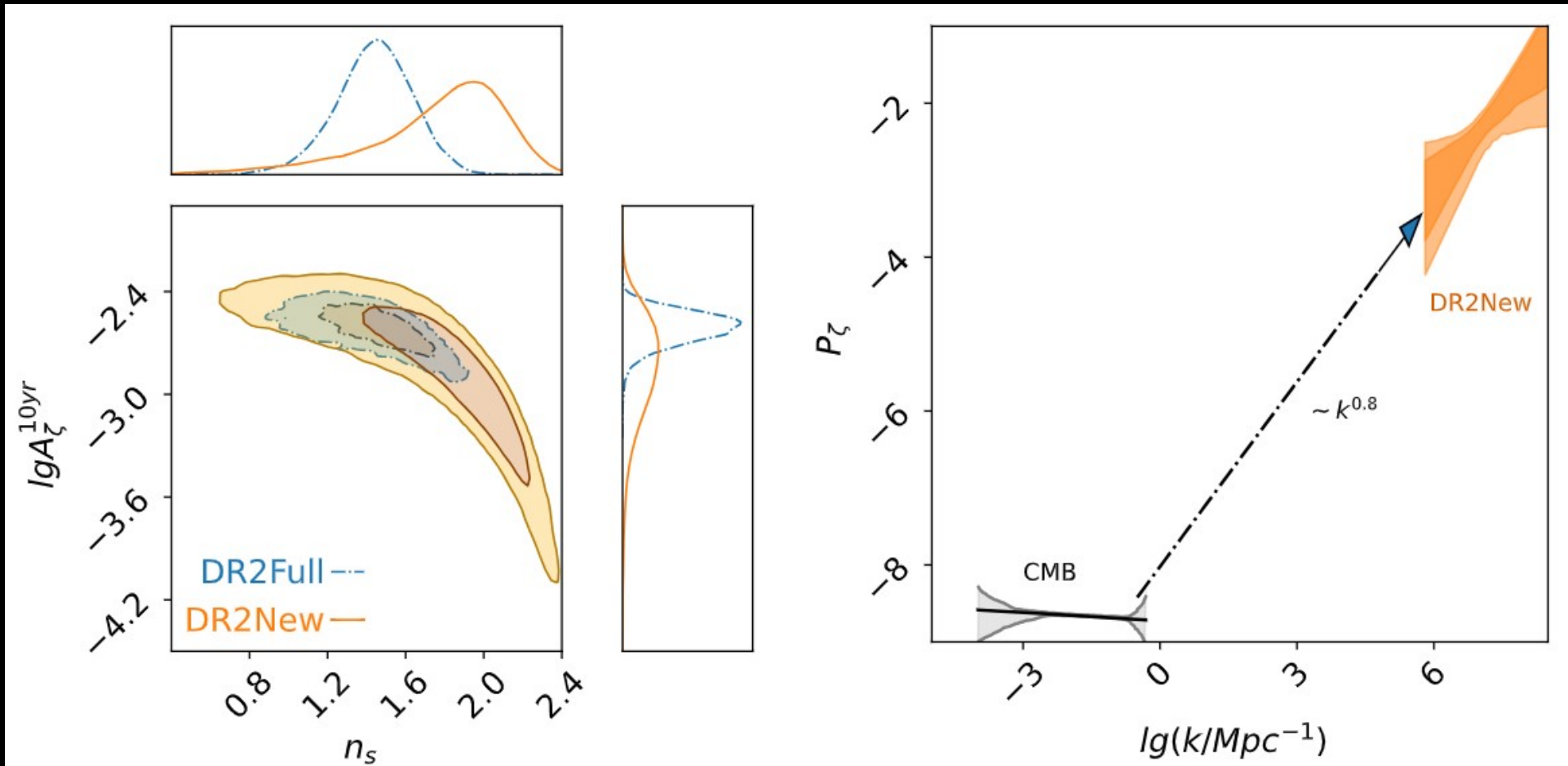
Early Universe: IV. Curvature perturbations

- Scalar perturbations in the early Universe seen in the CMB
- Can source GWs at second order

We assume a Power Law spectrum

$$P_{\zeta} = A_{\zeta}^{10\text{yr}} \left(\frac{k}{k_{10\text{yr}}} \right)^{(n_s-1)}$$

Excess at small scale must be invoked to not violate CMB constraints



Constraints on Ultra Light Dark Matter

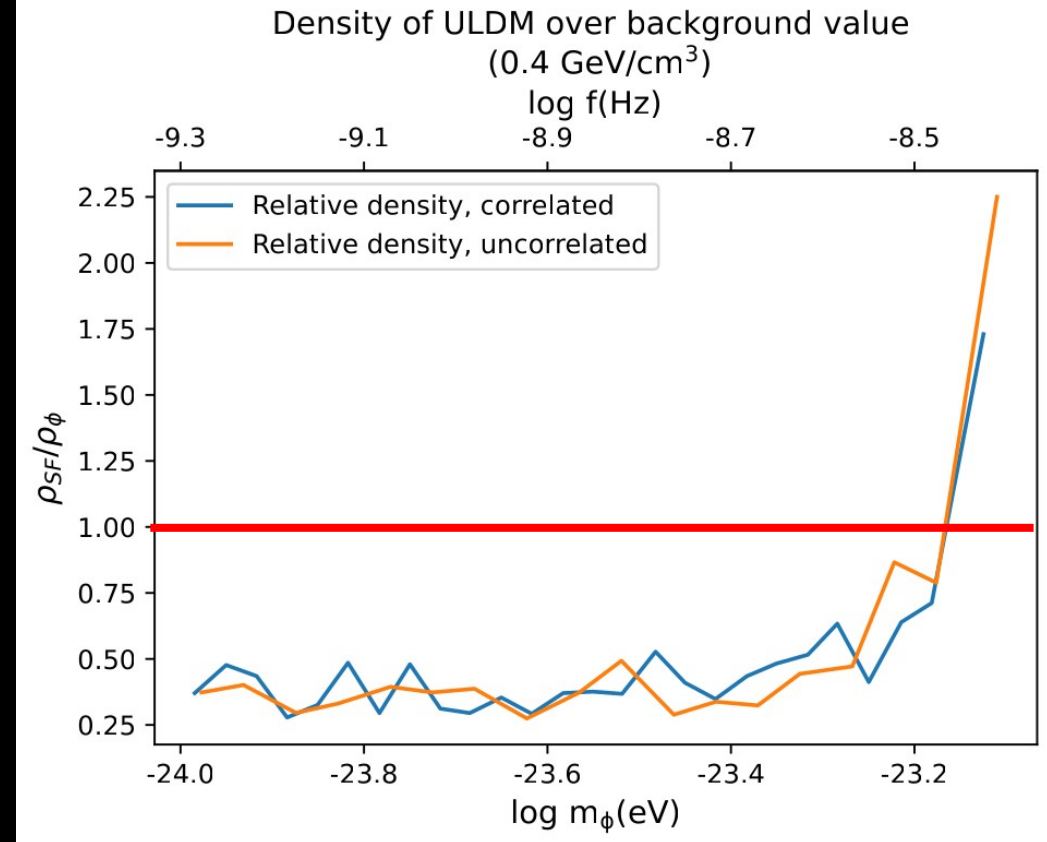
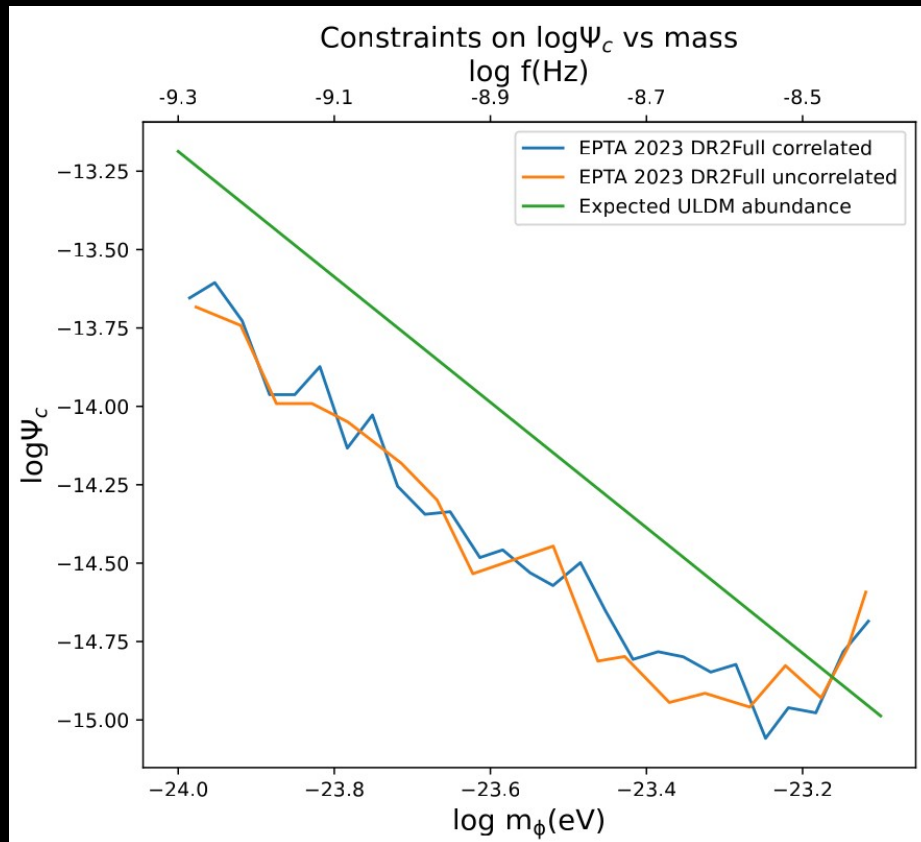
- Appealing dark matter candidate.
- Produces oscillations of the gravitational potential affecting the TOAs
- Effect depends on scalar field mass

-24 < m < -23.2 ruled out as DM in the solar neighborhood

$$\delta t = \frac{\Psi_c(\vec{x})}{2m_\phi} [\hat{\phi}_E^2 \sin(2m_\phi + \gamma_E) - \hat{\phi}_P^2 \sin(2m_\phi + \gamma_P)], \quad (3)$$

where

$$\frac{\Psi_c(\vec{x})}{10^{-18}} \approx 6.52 \left(\frac{10^{-22} \text{ eV}}{m_\phi} \right)^2 \left(\frac{\rho_\phi}{0.4 \text{ GeV/cm}^3} \right) \quad (4)$$



DOGGYBAG

- EPTA DR2 show a signal consistent with a GW origin (HD correlation)
- Hard to separate CGW from GWB
- signal broadly consistent with SMBHB origin
- SMBHB are massive and merge quickly
- Signal informative for galaxy formation models
- There's a number of processes in the Early Universe that can fit the data.
- First PTA constraints on fuzzy DM at some mass scale



